

Multidimensional Simulations of Convection Preceding a Type I X-ray Burst on the Surface of a Neutron Star

Chris Malone

SUNY Stony Brook

October 25th, 2010

Outline

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO
- 4 Our Results
- 5 Wrap-up

Topic

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO
- 4 Our Results
- 5 Wrap-up

Acknowledgements

Wetware

- Mike Zingale (SUNY Stony Brook)
- Ann Almgren, John Bell and Andy Nonaka (CCSE LBNL)
- Andrew Cumming (McGill University)
- Stan Woosley (UCSC)

Hardware

- franklin and hopper at LBNL's NERSC
- nyblue at BNL

What is a Type I X-ray Burst?

Properties

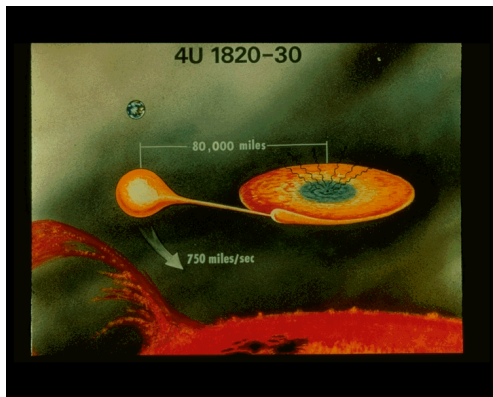
- Low Mass X-ray Binaries
- Accretion of H and/or He
- Ignition at base of accreted layer

$$E \sim 10^{39} \text{ ergs}$$

$$\tau_{\text{rise}} \sim \text{seconds}$$

$$\tau_{\text{dur.}} \sim 10\text{'s} - 100\text{'s seconds}$$

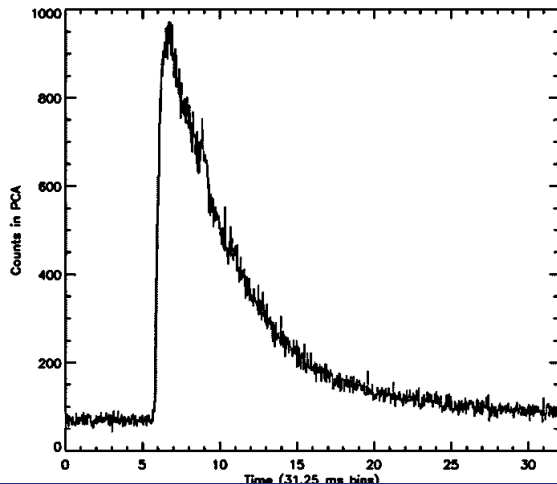
$$\tau_{\text{recur.}} \sim \text{hours to days}$$



heasarc.gsfc.nasa.gov/Images/exosat/slide_gifs/exosat18.gif

What is a Type I X-ray Burst?: Lightcurve

4U 1728-34

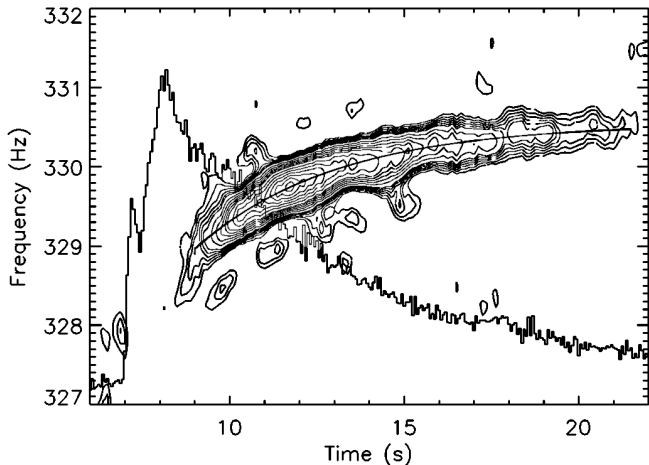


- Buring mode sets τ_{dur} .
- Inferred ignition column implies **deflagration** \rightarrow subsonic flow

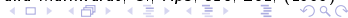
after
Strohmayer, T., et al., *ApJL*, 469, L9,
(1996)

What is a Type I X-ray Burst?: Oscillations

- Oscillations during rise – hot-spot spreading
- Oscillations during decay – unstable surface modes?

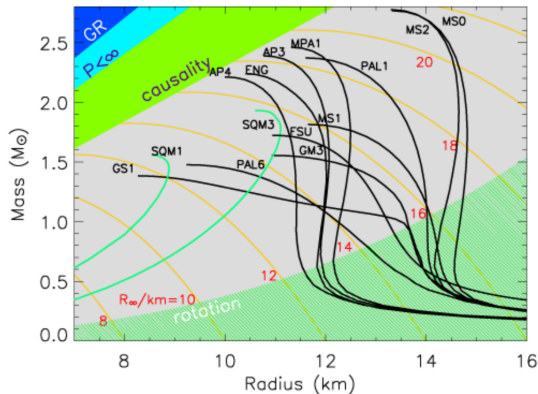


Strohmayer, T. and Markwardt, C., *ApJ*, 516, L81, (1999)



Why do we care?

- They are explosions!
- Unique location for rp-process burning
- Flame propagation under extreme conditions
- Possible distance indicators (?)
- Constrain EOS for dense matter



Lattimer, J.M., *ApSS*, 308, 371 (2007)

Topic

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO
- 4 Our Results
- 5 Wrap-up

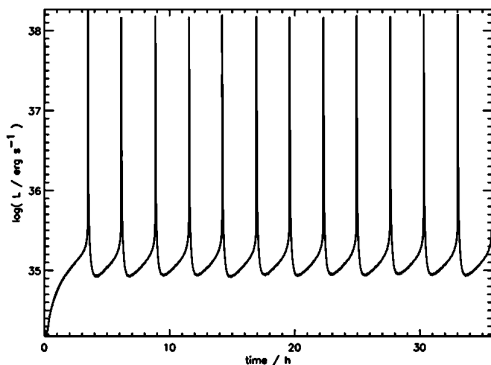
1-d Models of Type I X-ray Bursts

Pros

- Reproduce E , τ_{rise} , $\tau_{\text{dur.}}$, $\tau_{\text{recur.}}$
- Can use large reaction networks
- Computationally cheap

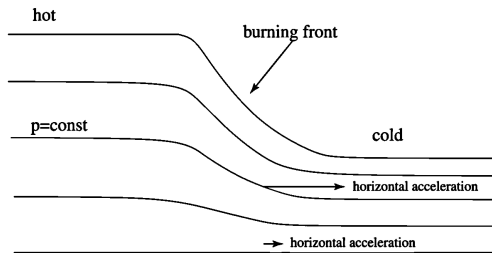
Cons

- Assume spherical symmetry
- Parameterized convection (MLT)
- Cannot study lateral flame propagation



Woosley et al., *ApJS*, 151, 75 (2004)

2-d Models of Type I X-ray Bursts



Spitkovsky et al., *ApJ*, 566, 1018 (2002)

- **Very few!!**
- Mostly treated as detonations—inconsistent with most observations
- Spitkovsky et al. used 2-layer, shallow water, incompressible, ideal gas to show importance of rotation

Modeling Type I X-ray Bursts

The problem domain is divided into zones, and discretized versions of the various conservation laws tell us how to evolve each zone over a small timestep.

Difficulty:

- Necessary condition for convergence of explicit hydrodynamics algorithm (CFL condition):
Information can not propagate more than one grid zone in a single timestep.

Modeling Type I X-ray Bursts

Information can not propagate more than one grid zone in a single timestep.

Compressible hydrodynamics (e.g. Euler equations)

Modeling Type I X-ray Bursts

Information can not propagate more than one grid zone in a single timestep.

Compressible hydrodynamics (e.g. Euler equations)

- Allows for sound waves

Modeling Type I X-ray Bursts

Information can not propagate more than one grid zone in a single timestep.

Compressible hydrodynamics (e.g. Euler equations)

- Allows for sound waves
- Information propagates at $U + c_s$:

$$\Delta t \lesssim \frac{\Delta x}{U + c_s}$$

Modeling Type I X-ray Bursts

Information can not propagate more than one grid zone in a single timestep.

Compressible hydrodynamics (e.g. Euler equations)

- Allows for sound waves
- Information propagates at $U + c_s$: $\Delta t \lesssim \frac{\Delta x}{U + c_s}$
- Supersonic (detonations; $M \equiv \frac{U}{c_s} \gg 1$): $\Delta t \lesssim \frac{\Delta x}{U}$

Modeling Type I X-ray Bursts

Information can not propagate more than one grid zone in a single timestep.

Compressible hydrodynamics (e.g. Euler equations)

- Allows for sound waves
- Information propagates at $U + c_s$:
- Supersonic (detonations; $M \equiv \frac{U}{c_s} \gg 1$):
- Subsonic (**deflagrations**; $M \ll 1$):

$$\Delta t \lesssim \frac{\Delta x}{U + c_s}$$

$$\Delta t \lesssim \frac{\Delta x}{U}$$

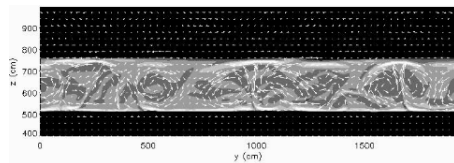
$$\Delta t \lesssim \frac{\Delta x}{c_s}$$

2-d Models of Type I X-ray Bursts

Low Mach Number Approximation Methods

- Filter acoustics—timestep size determined by *dynamics*:

$$\Delta t \lesssim \frac{\Delta x}{U}$$
- Factor of $1/M$ increase in timestep size
- Common example: incompressible fluid — $\nabla \cdot \mathbf{U} = 0$
- Can assume background/base state in HSE and consider motions about this state



Lin et al., *ApJ*, 653, 545 (2006)

Lin et al. low Mach number method

- Important first step
- 1st order accurate in space and time
- Didn't model top of atmosphere
- Time-independent base state

Topic

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO**
- 4 Our Results
- 5 Wrap-up

MAESTRO

as described in Nonaka et al., *ApJSS*, **188**, 358 (2010)

- Second order accurate in space and time
- Time-dependent base state
- Uses Adaptive Mesh Refinement
- Filters acoustics while retaining important compressible effects, such as stratification, thermal diffusion and composition change

Filtering Acoustics

MAESTRO low Mach number equation set

- Decompose pressure field: $p(\mathbf{x}, r, t) = p_0(r, t) + \pi(\mathbf{x}, r, t)$

Filtering Acoustics

MAESTRO low Mach number equation set

- Decompose pressure field: $p(\mathbf{x}, r, t) = p_0(r, t) + \pi(\mathbf{x}, r, t)$
- Base state density: $\nabla p_0 = -g\rho_0 \mathbf{e}_r$



Filtering Acoustics

MAESTRO low Mach number equation set

- Decompose pressure field: $p(\mathbf{x}, r, t) = p_0(r, t) + \pi(\mathbf{x}, r, t)$
- Base state density: $\nabla p_0 = -g\rho_0 \mathbf{e}_r$
- Asymptotic expansion of hydro eqns in M : $\frac{|\pi|}{p_0} = \mathcal{O}(M^2)$



Filtering Acoustics

MAESTRO low Mach number equation set

- Decompose pressure field: $p(\mathbf{x}, r, t) = p_0(r, t) + \pi(\mathbf{x}, r, t)$
- Base state density: $\nabla p_0 = -g\rho_0 \mathbf{e}_r$
- Asymptotic expansion of hydro eqns in M : $\frac{|\pi|}{p_0} = \mathcal{O}(M^2)$

$$\frac{\partial(\rho X_k)}{\partial t} = -\nabla \cdot (\rho X_k \mathbf{U}) + \rho \dot{\omega}$$

$$\frac{\partial \mathbf{U}}{\partial t} = -\mathbf{U} \cdot \nabla \mathbf{U} - \frac{1}{\rho} \nabla \pi - \frac{\rho - \rho_0}{\rho} g \mathbf{e}_r$$

$$\frac{\partial(\rho h)}{\partial t} = -\nabla \cdot (\rho h \mathbf{U}) + \frac{Dp_0}{Dt} + \rho H_{\text{nuc}} + \nabla \cdot (\kappa \nabla T)$$

$$\nabla \cdot (\beta_0 \mathbf{U}) = \beta_0 \left(S - \frac{1}{\bar{\Gamma}_1 p_0} \frac{\partial p_0}{\partial t} \right)$$



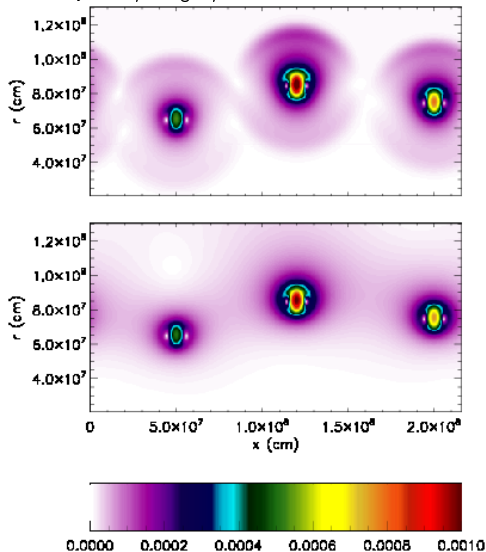
Filtering Acoustics

- compressible

- MAESTRO

Mach Number

astro.sunysb.edu/mzingale/Maestro



Topic

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO
- 4 Our Results**
- 5 Wrap-up

Initial 1-d Model Generation

Discussed in Malone et al., (2010) submitted to ApJ

- Construct simple atmosphere in HSE and thermal equilibrium;
(similar to Cumming & Bildsten, *ApJ*, 544, 453 (2000))

$$\frac{dT}{dy} = \frac{3\kappa}{4acT^3} F$$

$$\frac{dF}{dy} = 0$$

where $dy = -\rho dr$ with y as column depth

- Include constant heat flux from deep crustal heating:
 $F = 200 \text{ keV / nucleon}$
- Base should be thermally unstable: $\frac{d\epsilon_{\text{nuc}}}{dT} > \frac{d\epsilon_{\text{cool}}}{dT}$
- Typically ϵ_{cool} is approximated as $\epsilon_{\text{cool}} \approx \frac{acT^4}{3\kappa y^2}$

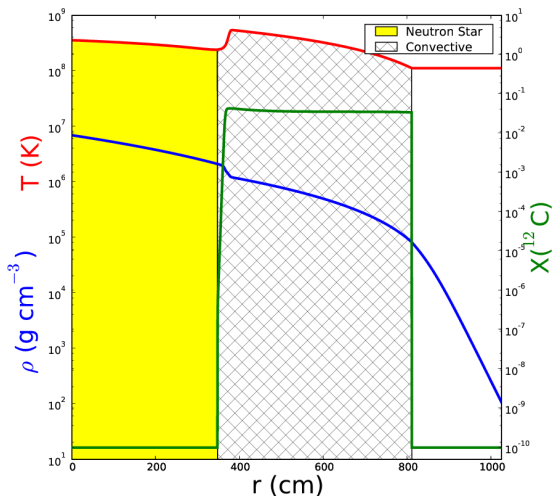
Initial 1-d Model Generation

When mapping to multi-d:

- System can cool from convective overturn
- Approximation to cooling needs to be augmented for the system to be unstable

$$\epsilon_{\text{cool}} \approx \frac{acT^4}{3\kappa y^2} + \epsilon_{\text{conv.}}$$

- Effective convective cooling provided MLT in the Kepler code (thanks to Stan Woosley)



Onwards toward Multi-d...

- 1-d model is laterally mapped across multi-d domain
- No multi-d velocity information from Kepler
- Symmetry broken by small ($\Delta T/T \sim 10^{-5}$) perturbation—this seeds convection

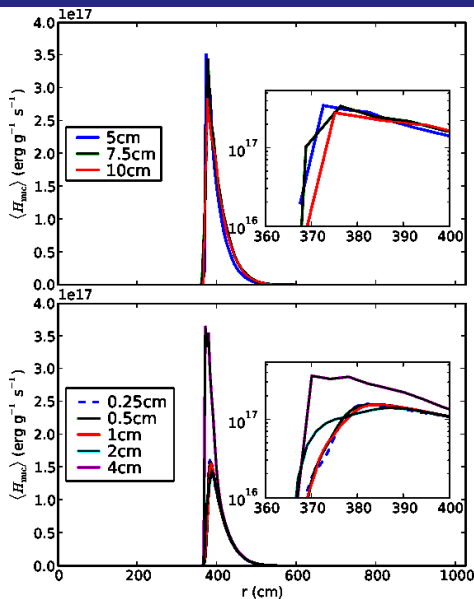
This Study

- We assumed pure ${}^4\text{He}$ accretion (similar to 4U 1820–30) ontop of a pure ${}^{56}\text{Fe}$ neutron star substrate.
- We only included forward and reverse 3α burning rates from Caughlan & Fowler (1988).

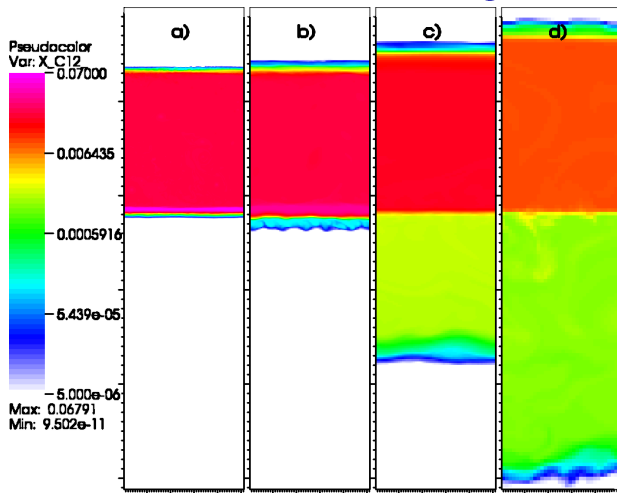
Resolution Studies

Resolution issues

- Sharp jump in T creates very peaked $H_{\text{nuc}}(\sim T^{40})$
- Requires high resolution (~ 0.5 cm / zone) to resolve thin burning layer
- Comparison: Lin et al. used 5 cm / zone
note their model used a pure ^{12}C substrate and had a much smoother thermal profile



Resolution Studies: Under-resolving=BAD!



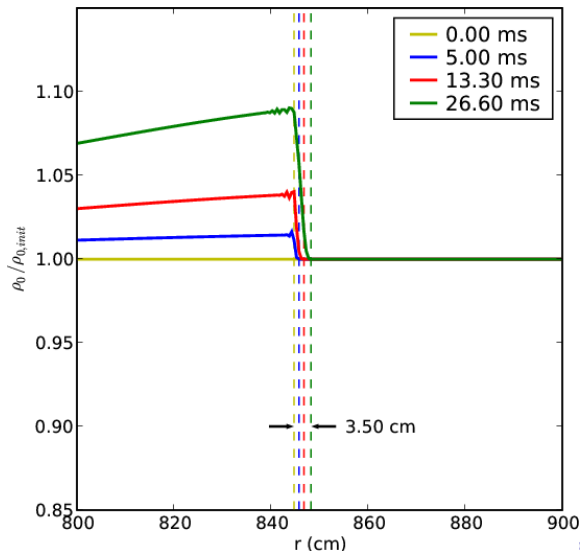
a) 0.5 cm zone^{-1} ; b) 2 cm zone^{-1} ; c) 4 cm zone^{-1} ; d) 7.5 cm zone^{-1}



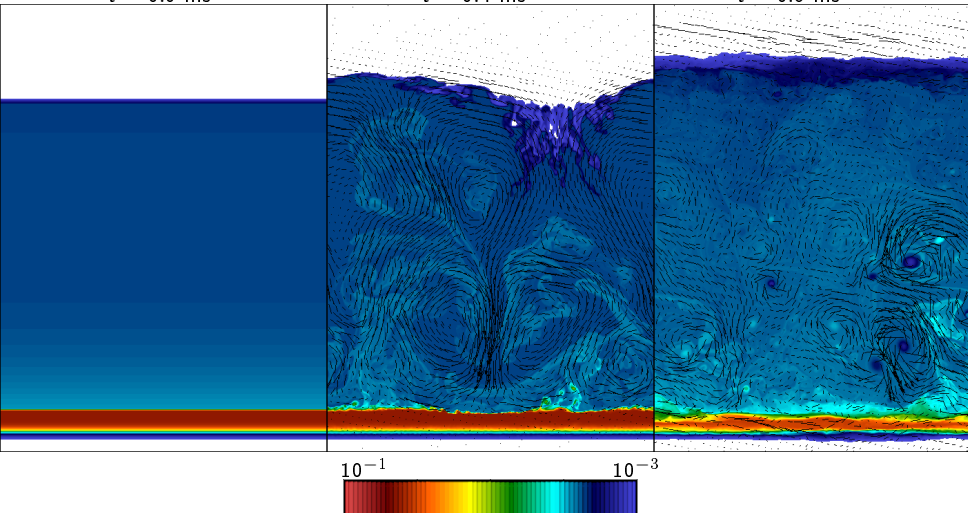
Expansion of Atmosphere

With MAESTRO we can model the surface of the star without numerical complications.

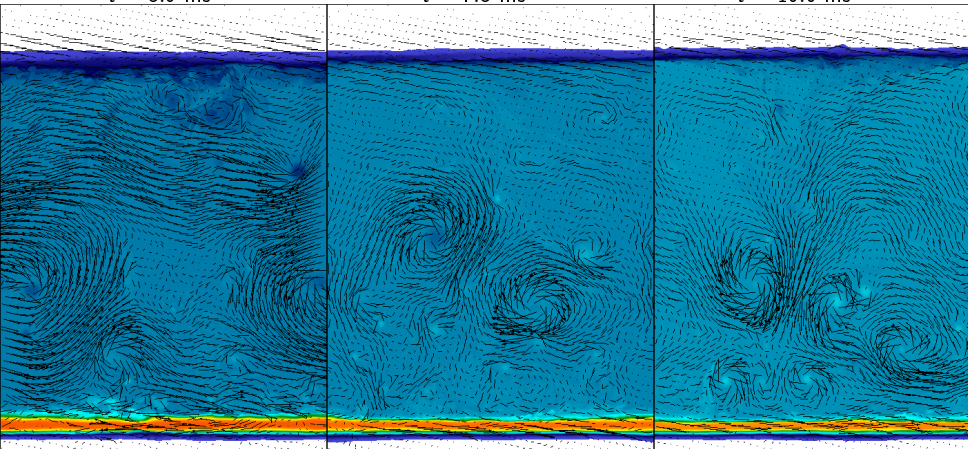
Furthermore, we use a **time-dependent** base state, which allows us to capture the expansion of the atmosphere from heating.



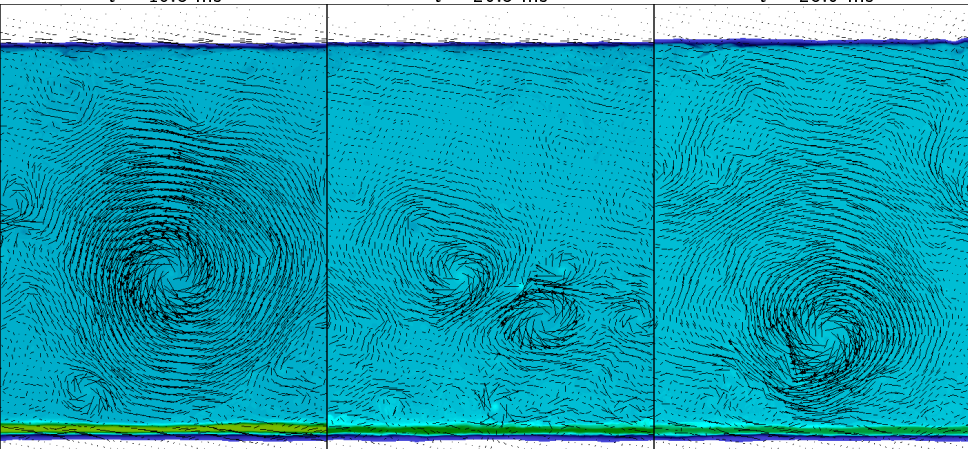
Convective Dynamics: $X(^{12}\text{C})$ and Velocity Vectors

 $t = 0.0 \text{ ms}$ $t = 0.4 \text{ ms}$ $t = 0.8 \text{ ms}$ 

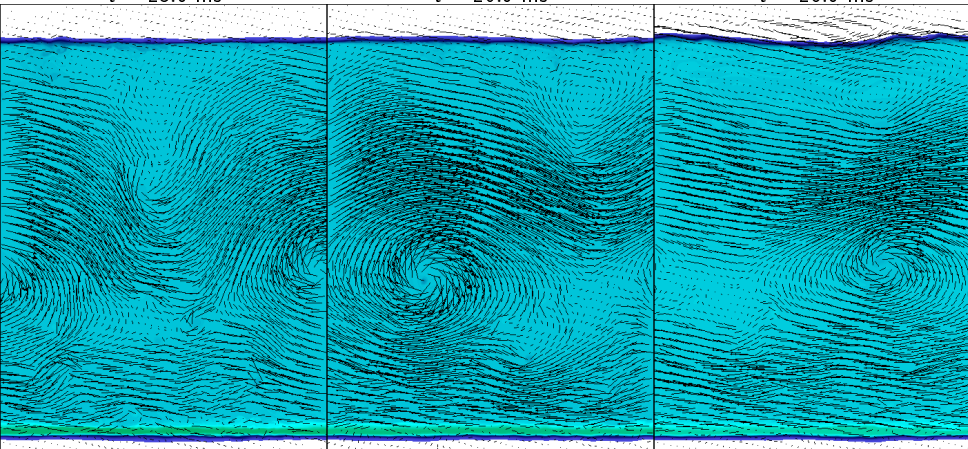
Convective Dynamics: $X(^{12}\text{C})$ and Velocity Vectors

 $t = 5.0 \text{ ms}$ $t = 7.5 \text{ ms}$ $t = 10.0 \text{ ms}$ 

Convective Dynamics: $X(^{12}\text{C})$ and Velocity Vectors

 $t = 18.5 \text{ ms}$ $t = 20.5 \text{ ms}$ $t = 23.0 \text{ ms}$ 

Convective Dynamics: $X(^{12}\text{C})$ and Velocity Vectors

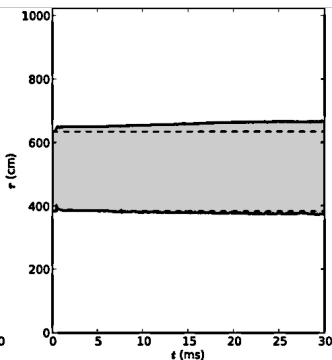
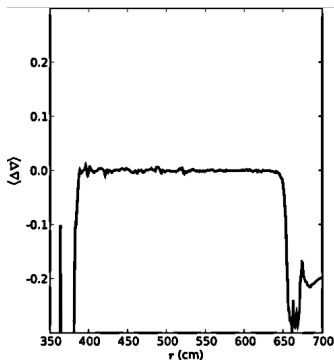
 $t = 25.0 \text{ ms}$ $t = 26.0 \text{ ms}$ $t = 28.0 \text{ ms}$ 

Convective Dynamics: Extent of Convective Region

Adiabatic Excess

$$\Delta\nabla = \frac{\nabla(\ln T) \cdot \mathbf{e}_r}{\nabla(\ln p) \cdot \mathbf{e}_r} - \left(\frac{d \ln T}{d \ln p} \right)_s$$

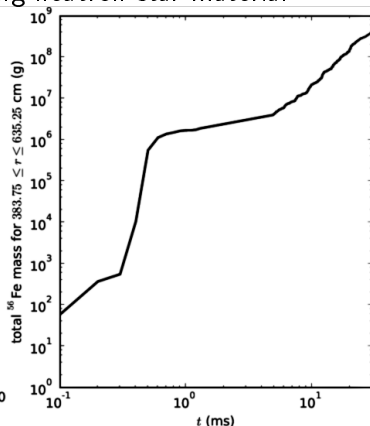
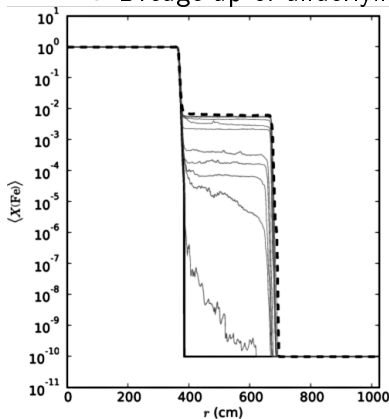
$t = 7.9$ ms



Upper boundary expands upward by 32.5 cm; lower boundary expands downward by 9.5 cm

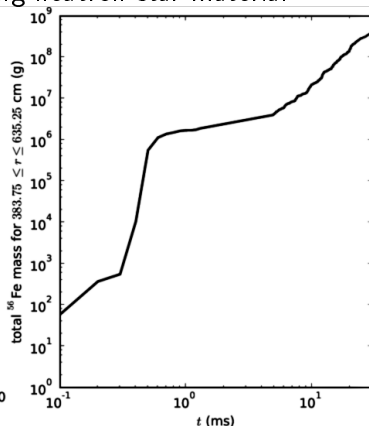
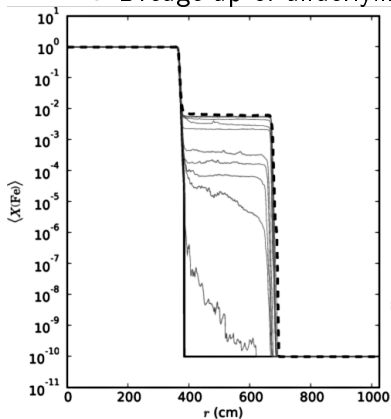
Convective Dynamics: Iron Dredge-up

- Eddies interact with lower convective boundary
- Shearing occurs
- Dredge-up of underlying neutron star material



Convective Dynamics: Iron Dredge-up

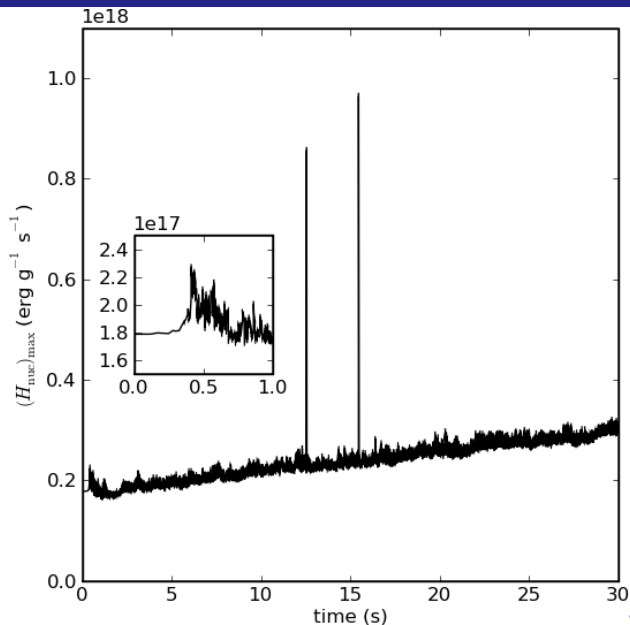
- Eddies interact with lower convective boundary
- Shearing occurs
- Dredge-up of underlying neutron star material



This affects
conductivity!

Energy Generation

- Still linear—no flame ignition yet
- Interesting short-lived spikes when turbulence brings fresh fuel to hotter layers



Topic

- 1 Introduction
- 2 Past numerical studies
- 3 Computational Method of our Code, MAESTRO
- 4 Our Results
- 5 **Wrap-up**

Wrap-up

Conclusions

- For a system that is close to runaway in mult-d, ϵ_{cool} needs to include convective terms.
- Our models suggest an order of magnitude more resolution than what has been used previously.
- The strong convection interacts with and churns up the underlying neutron star material.

Future Work

- Investigate different initial models—maybe relax resolution requirement
- Investigate mixed H/He bursts—maybe relax resolution requirement
- Compare 3-d runs with 2-d runs—does dredge-up still occur?

