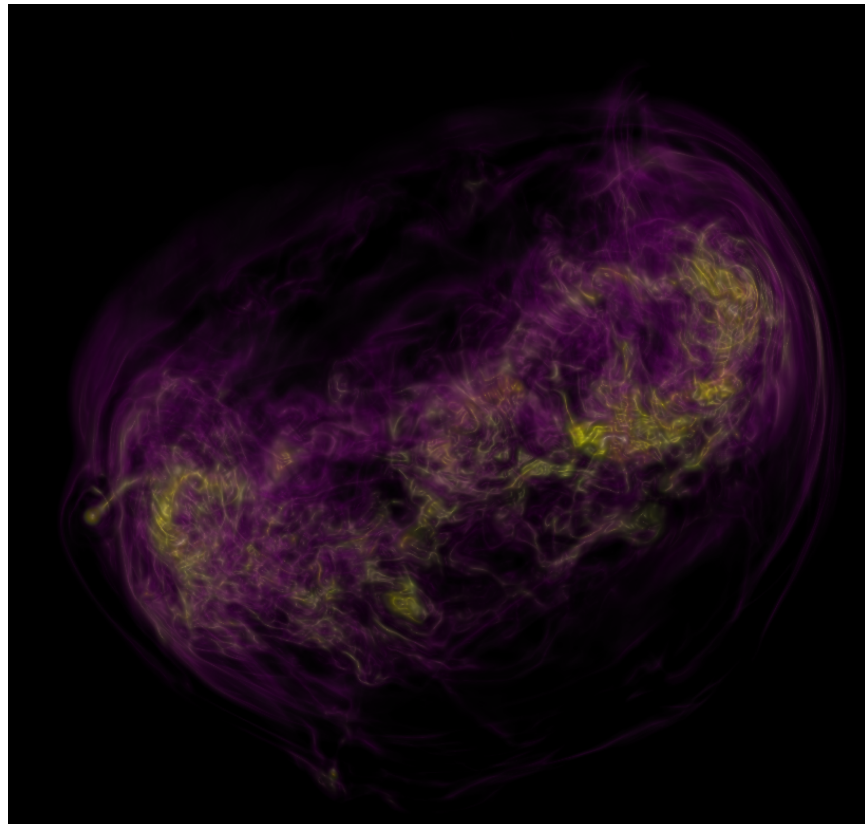


# Toward End-to-End Simulation of SNe Ia

Chris Malone



Department of Astronomy and Astrophysics  
UCSC

April 16<sup>th</sup>, 2013

# Acknowledgments

## Wetware

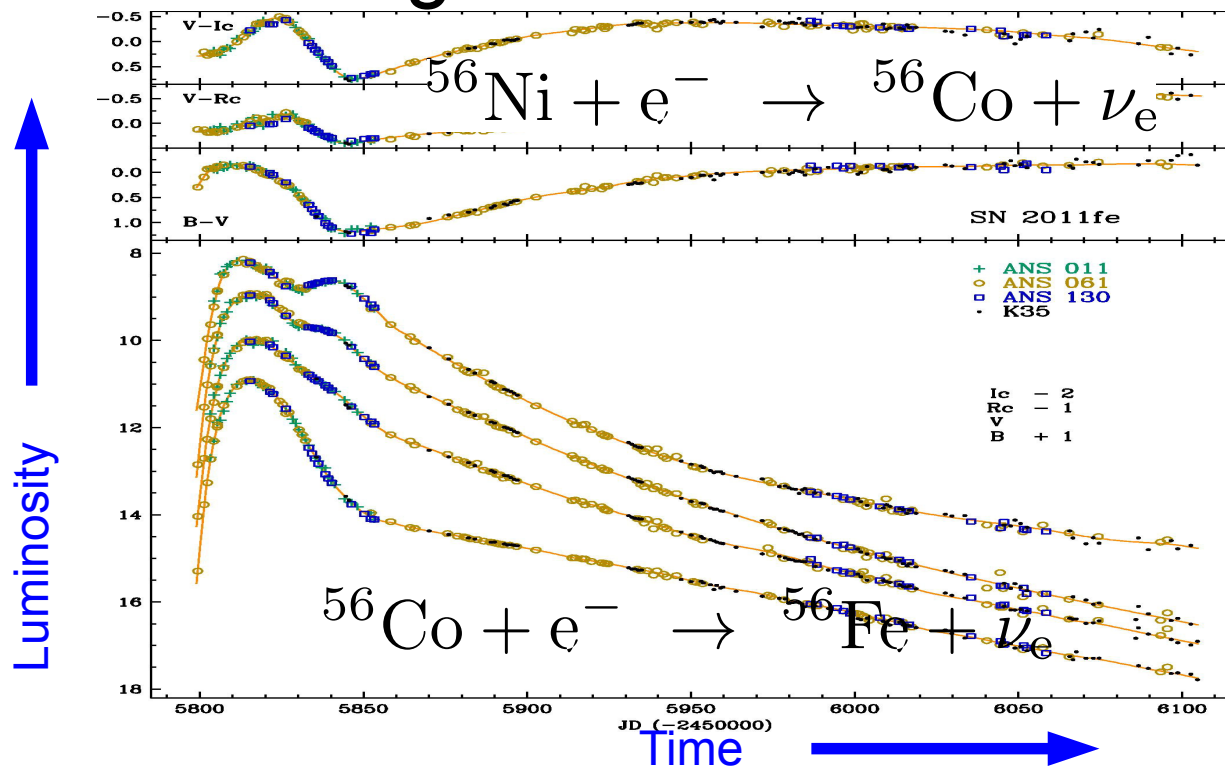
- UCSC
  - + Stan Woosley
  - + Shawfeng Dong
- SUNY Stony Brook
  - + Mike Zingale
- LBNL
  - + Ann Almgren
  - + John Bell
  - + Andy Nonaka

## Hardware

- NERSC
  - + Hopper
- OLCF
  - + Jaguar
  - + Titan
- NCSA
  - + Blue Waters

# What is a SN Ia?

- Transient event visible for months to years
- “I” means no significant Hydrogen
- “a” means strong Silicon lines



SN2011fe

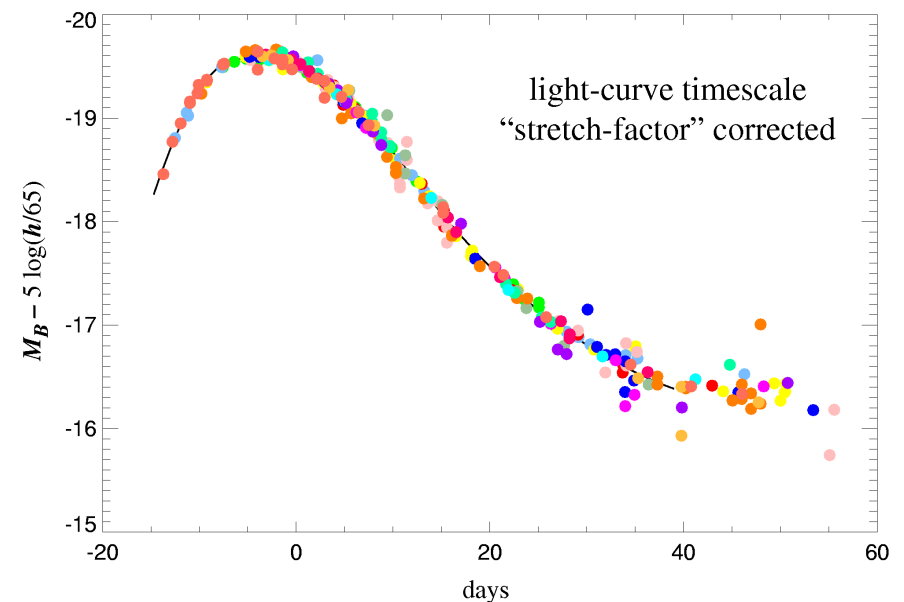
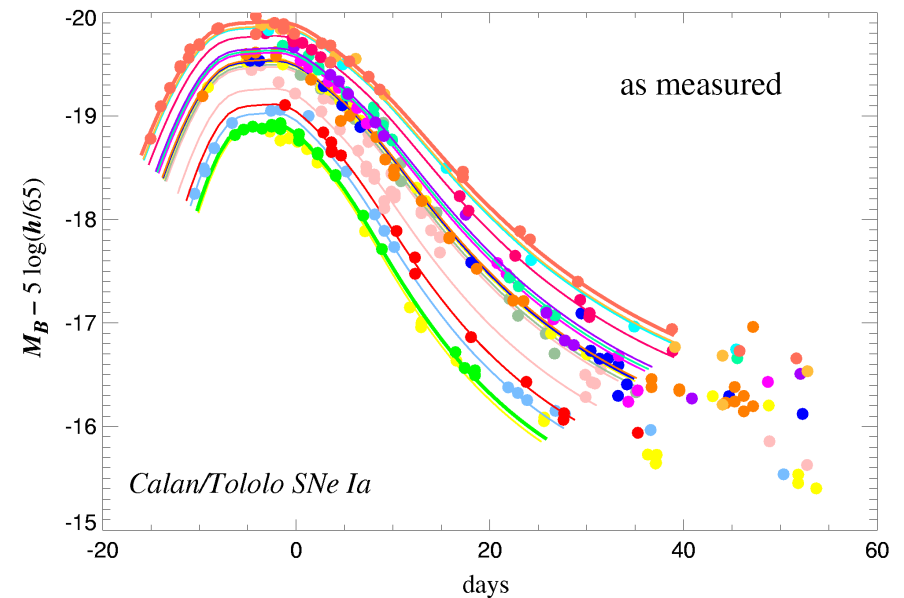
Munari+  
2013

# Standard(izable) Candles

- “Broader is brighter” – Phillips relation
- SN lightcurve width related to intrinsic brightness
- Allows for distance measure

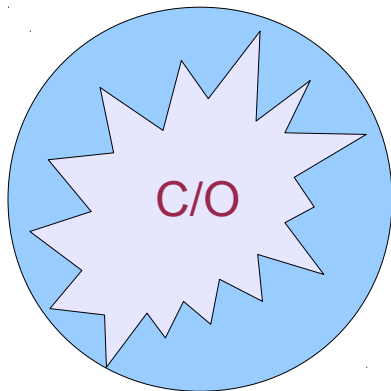
2011 Nobel Prize in Physics:  
Perlmutter, Schmidt, and Riess

“for the discovery of the accelerating expansion of the Universe through observations of distant supernovae.”

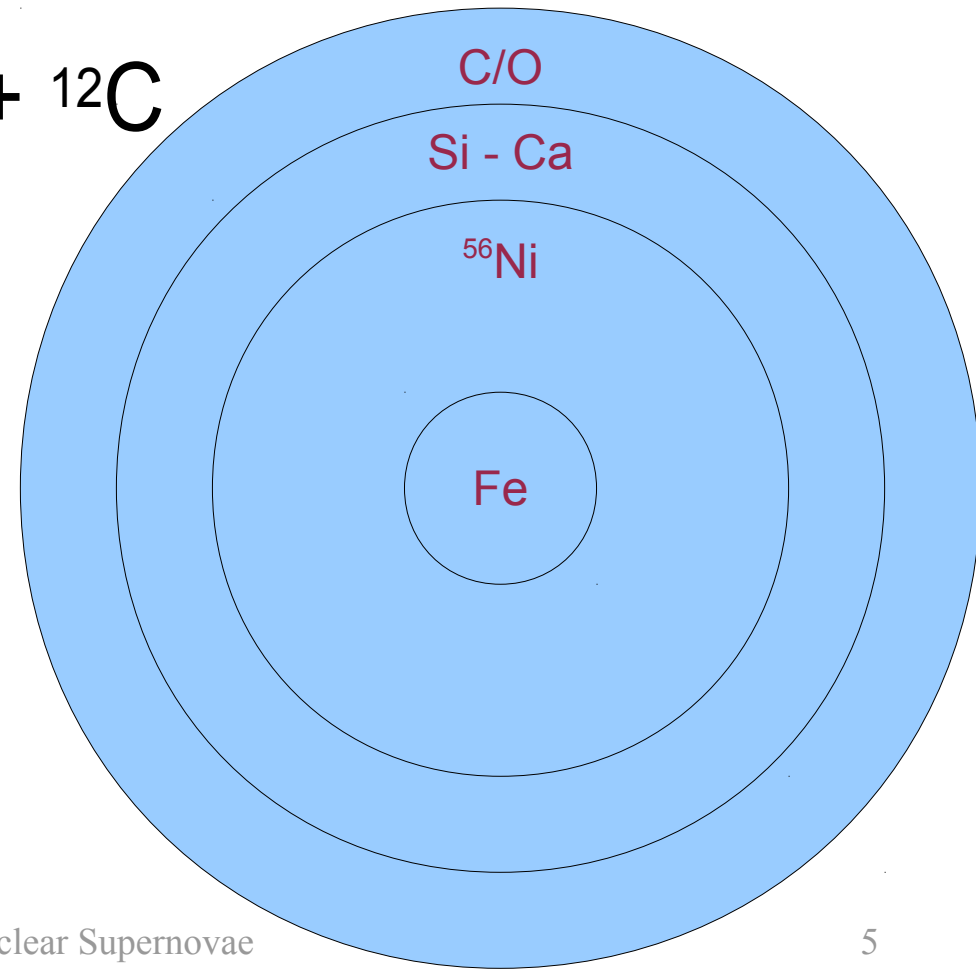


# Single Degenerate Model

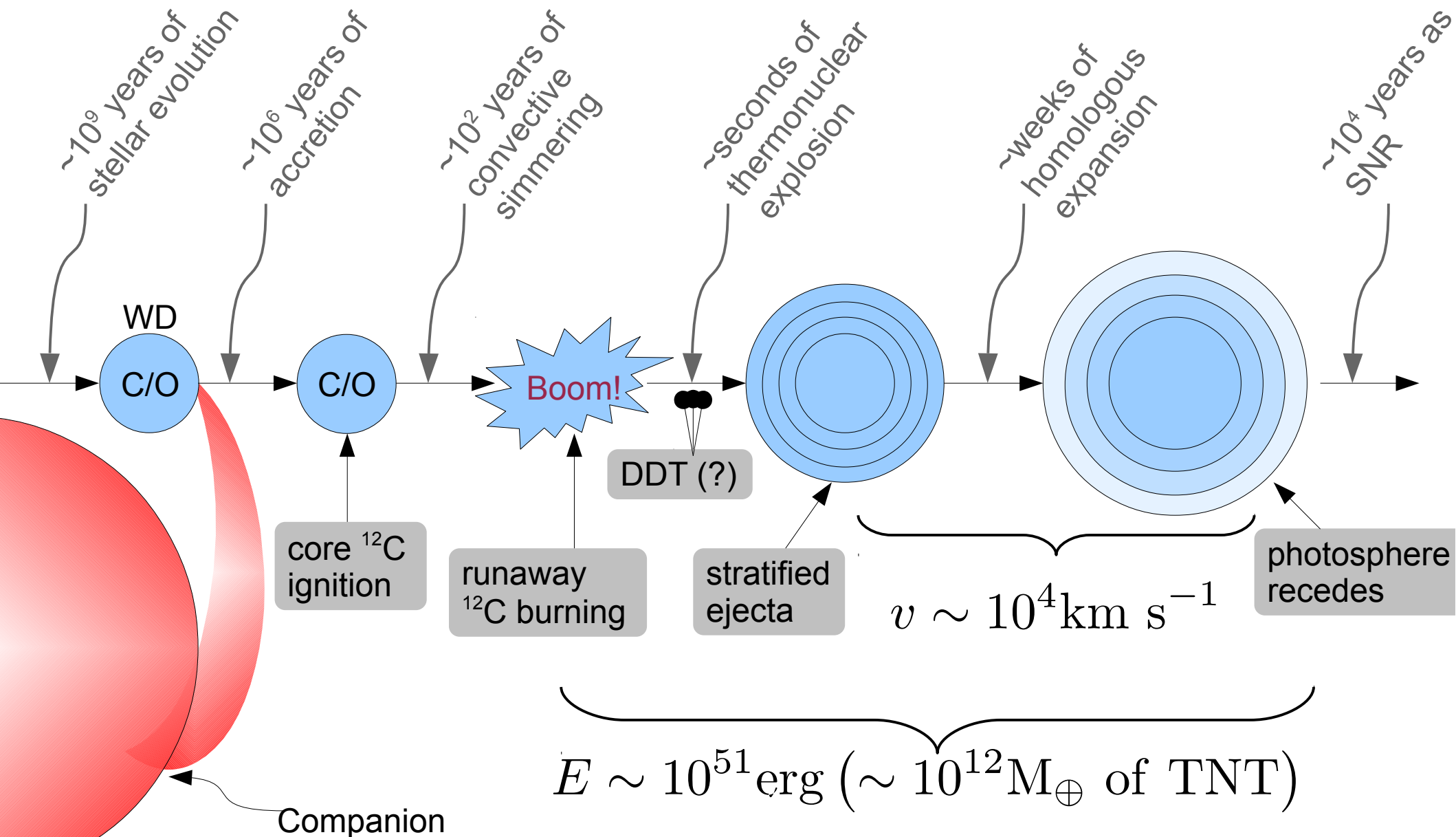
- C/O WD + companion
- WD approaches Chandrasekhar mass ( $\sim 1.4M_{\odot}$ )
- Core carbon fusion,  $^{12}\text{C} + ^{12}\text{C}$
- Centuries of convection



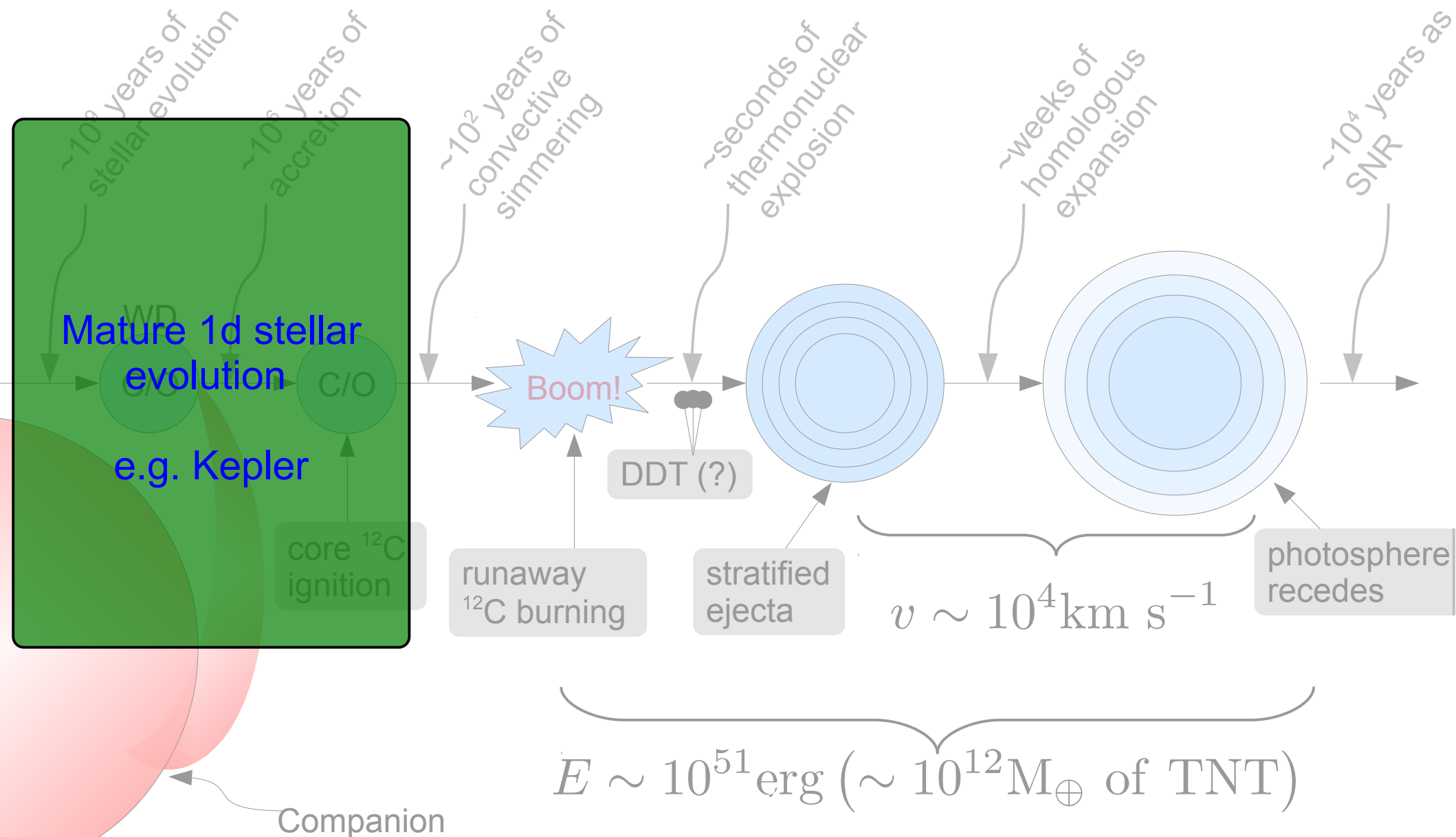
BOOM!



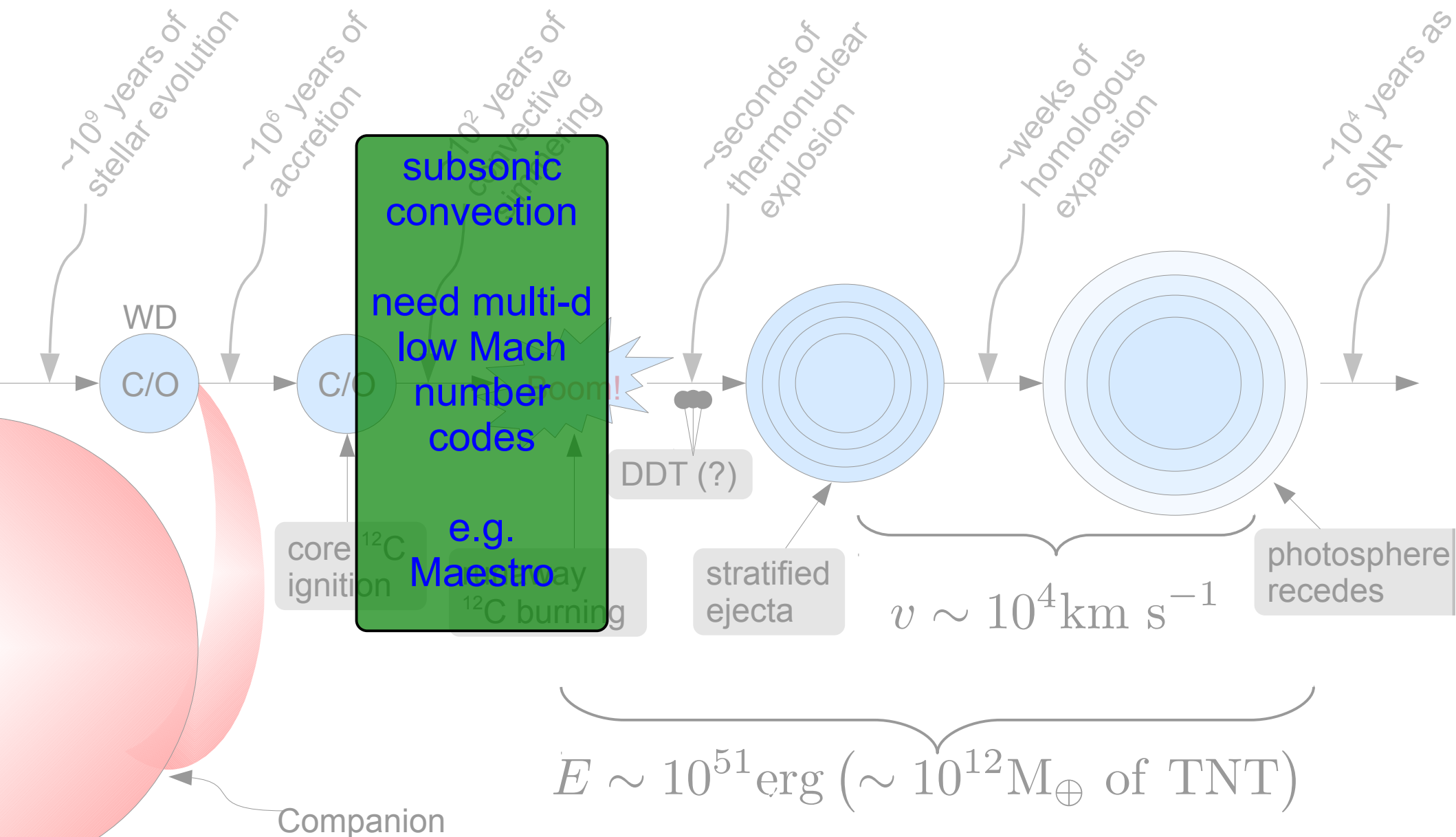
# Single Degenerate Model



# Single Degenerate Model

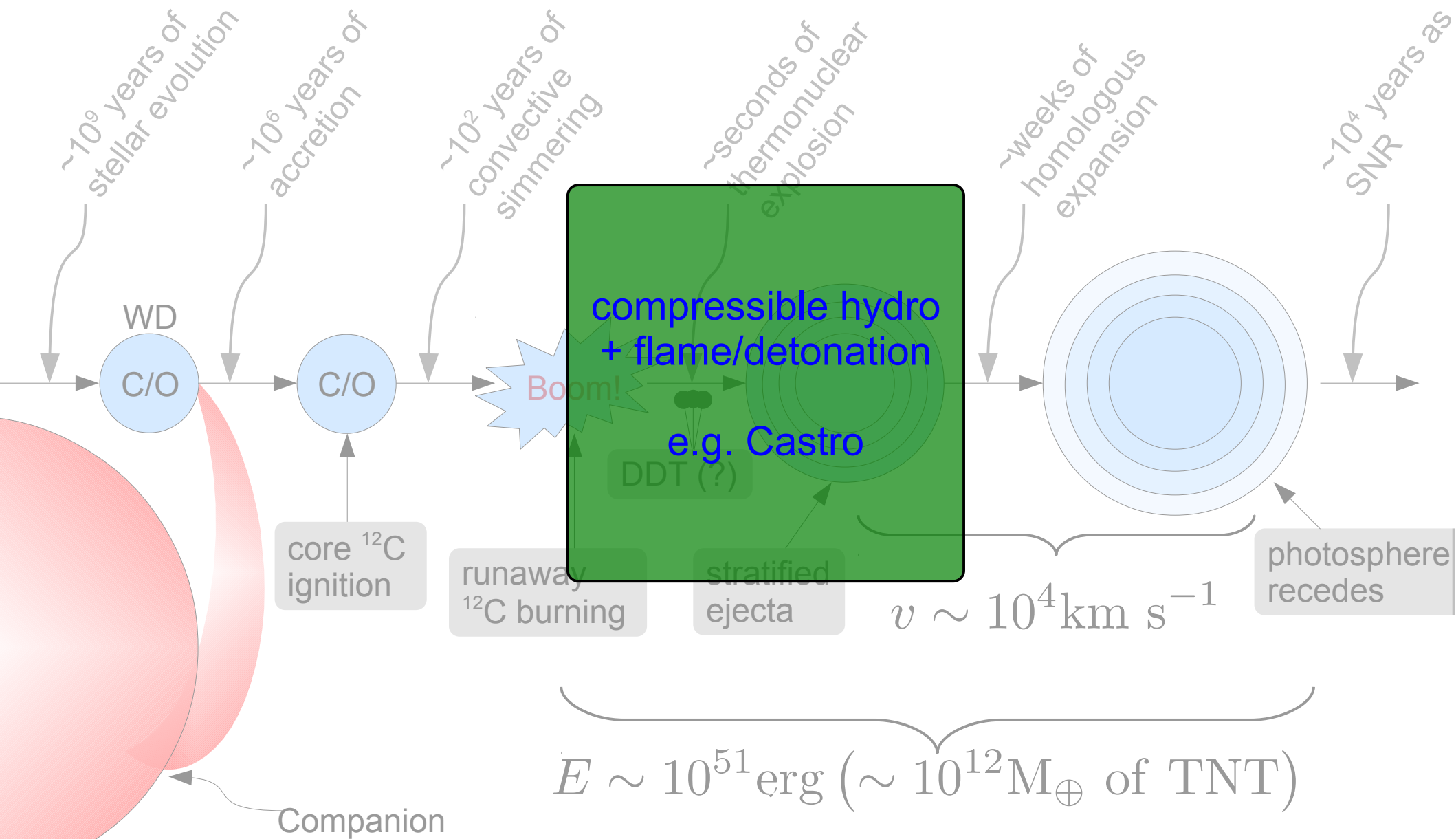


# Single Degenerate Model

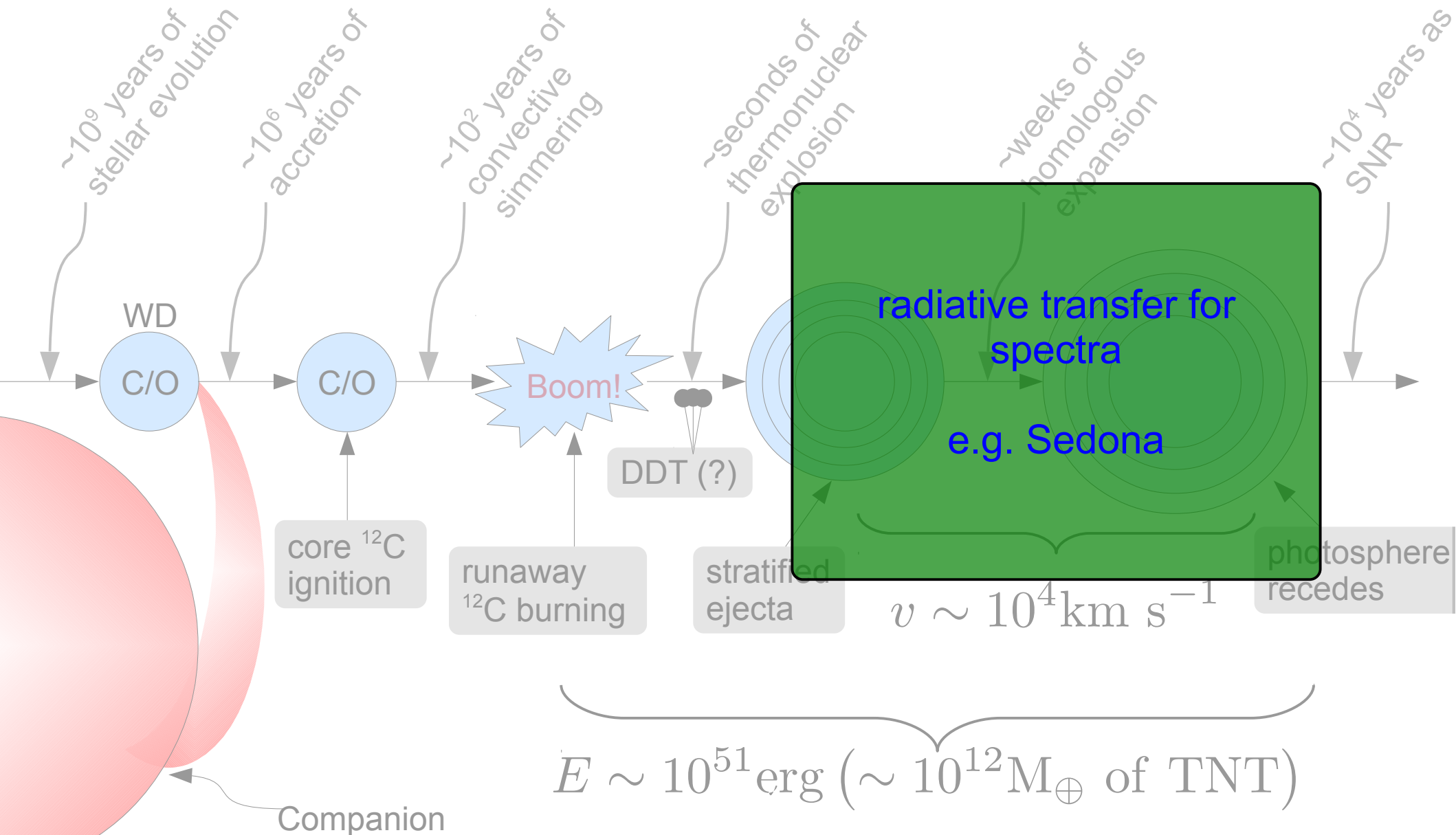




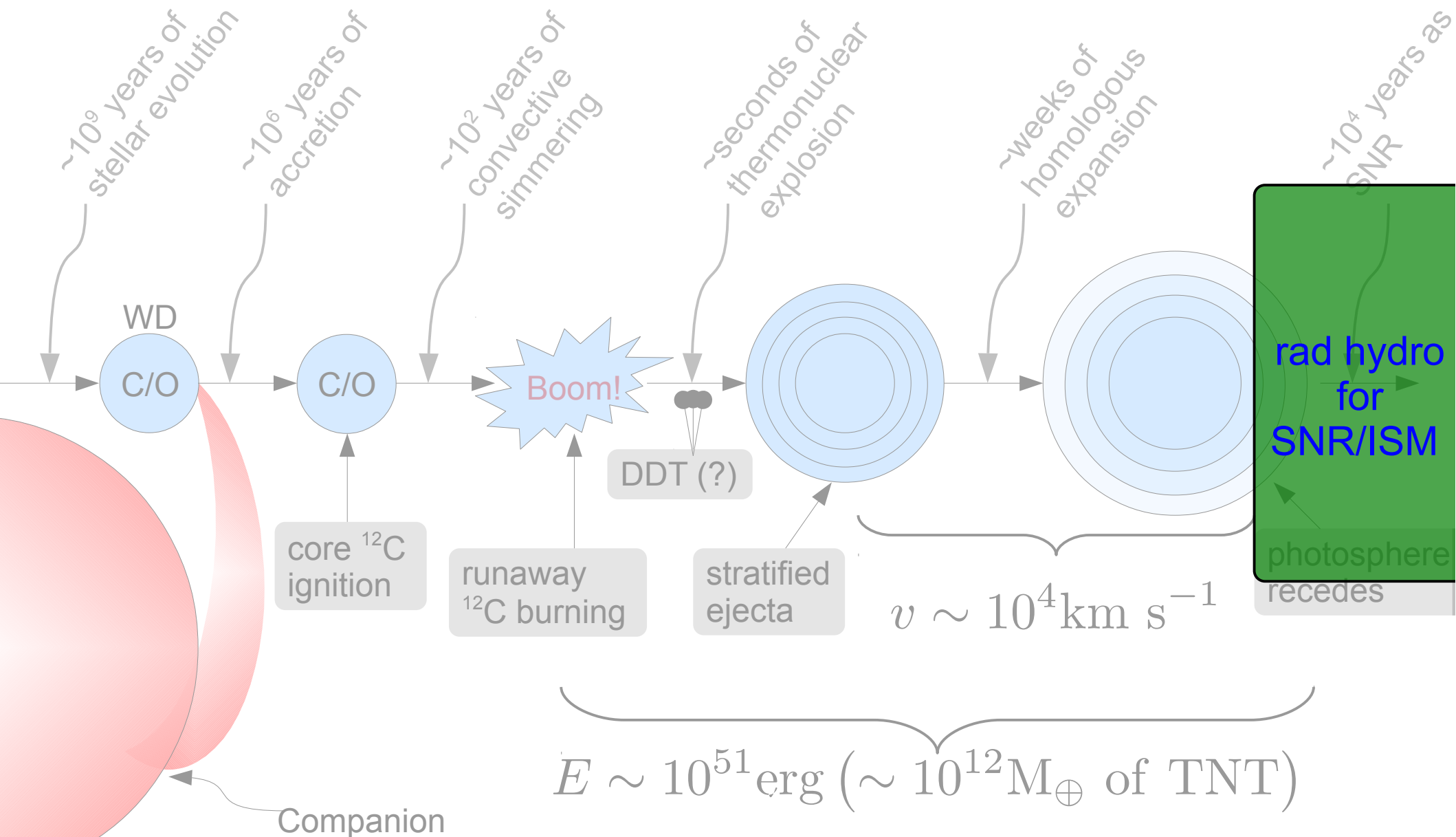
# Single Degenerate Model



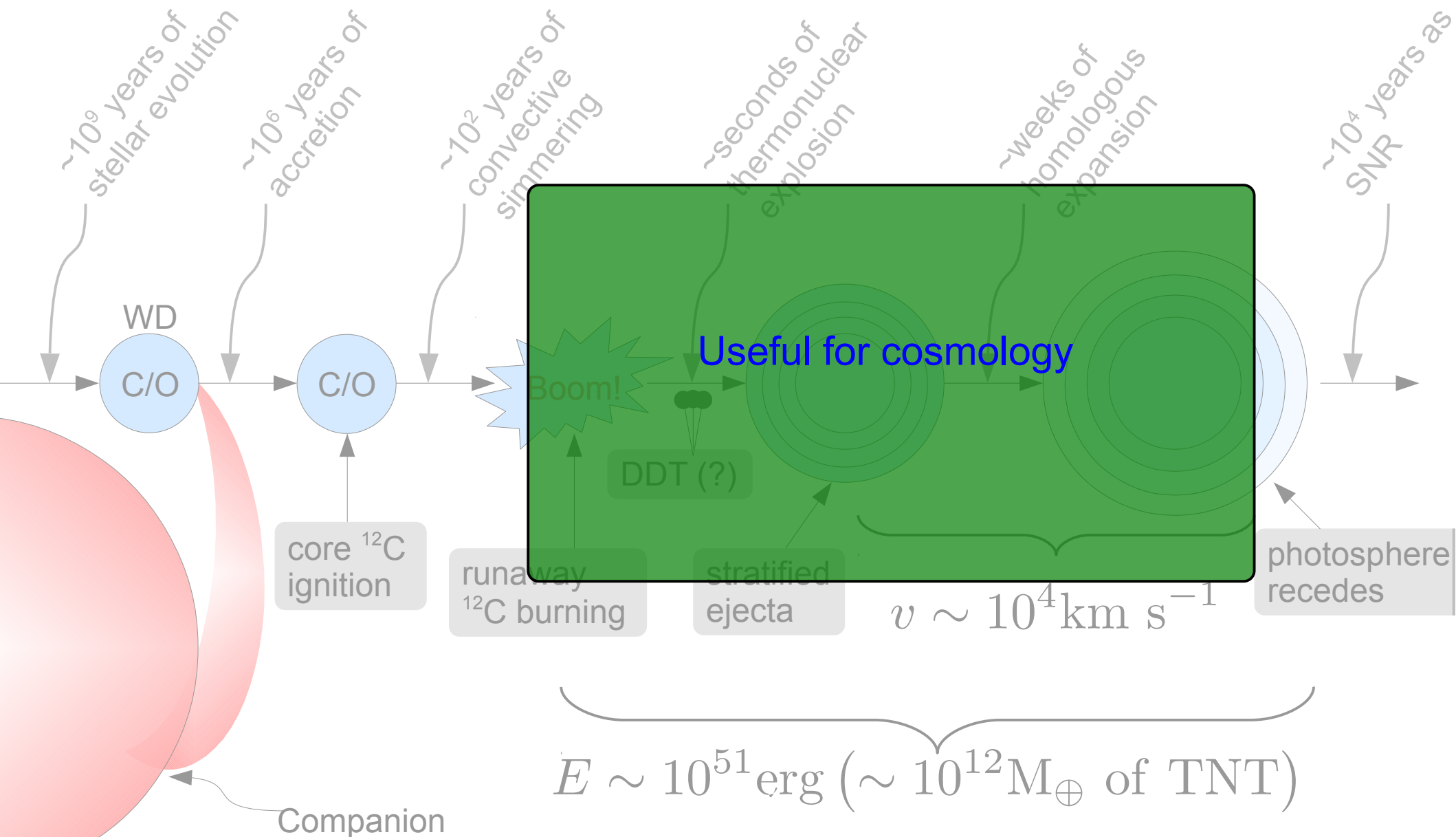
# Single Degenerate Model



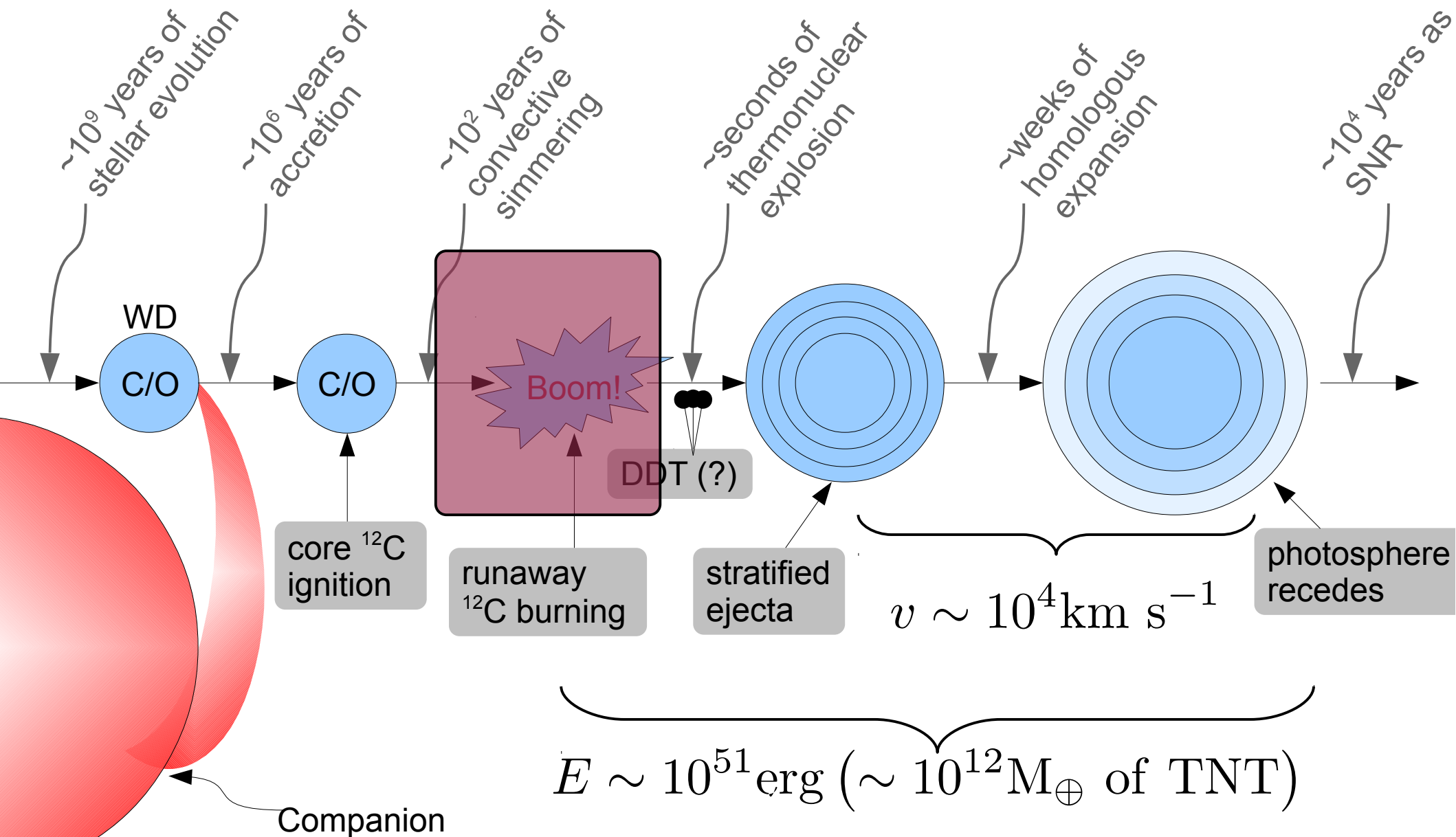
# Single Degenerate Model



# Single Degenerate Model



# Single Degenerate Model

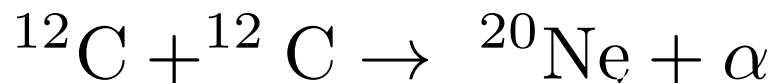


# Centuries of Simmering

- Compression heats core

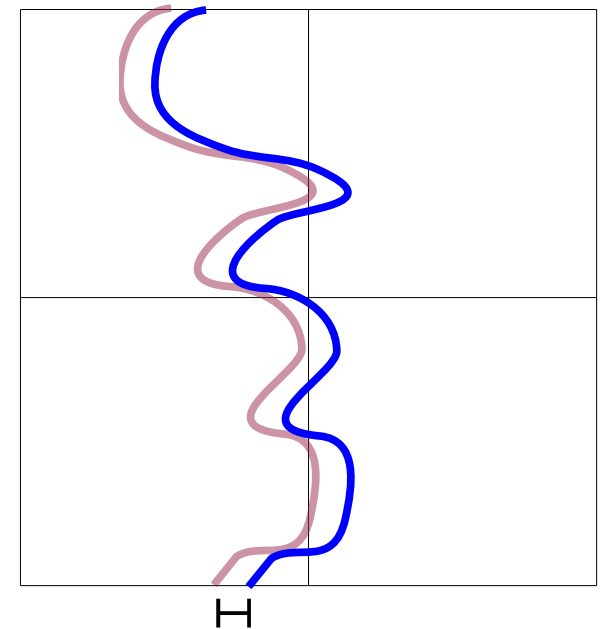
$$\rho_c \sim 2 \times 10^9 \text{ g cm}^{-3} \quad T_c \sim 4 \times 10^8 \text{ K}$$

- Core carbon burning drives low Mach number convection ( $M \sim 0.01$ )



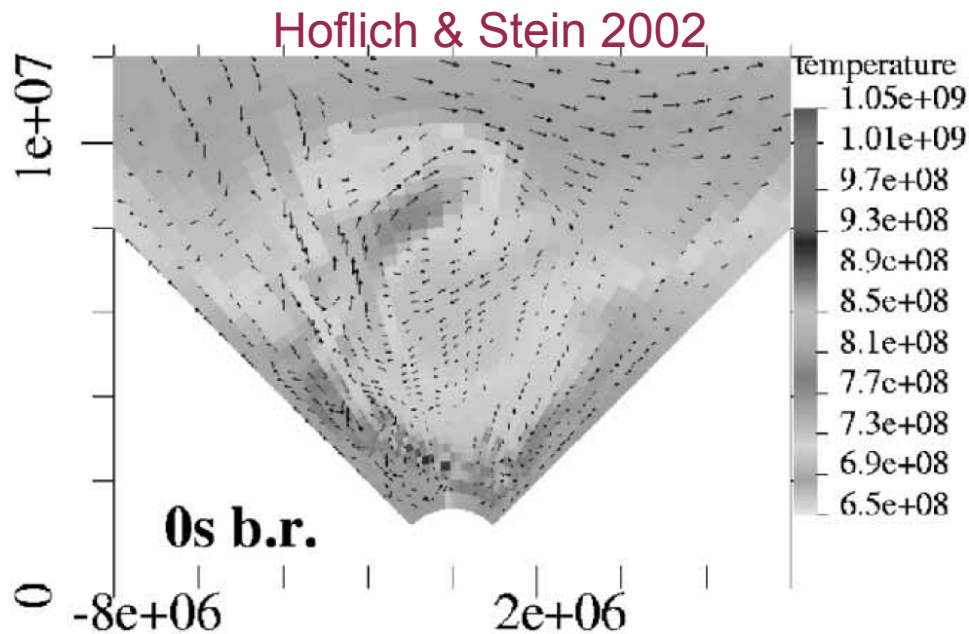
- Efficient simulation requires special care because of CFL condition

$$\Delta t_{\text{CFL}} \lesssim \frac{\Delta x}{U_{c,\text{max}}} \xrightarrow{(M \ll 1)} \frac{\Delta x}{c_s}$$



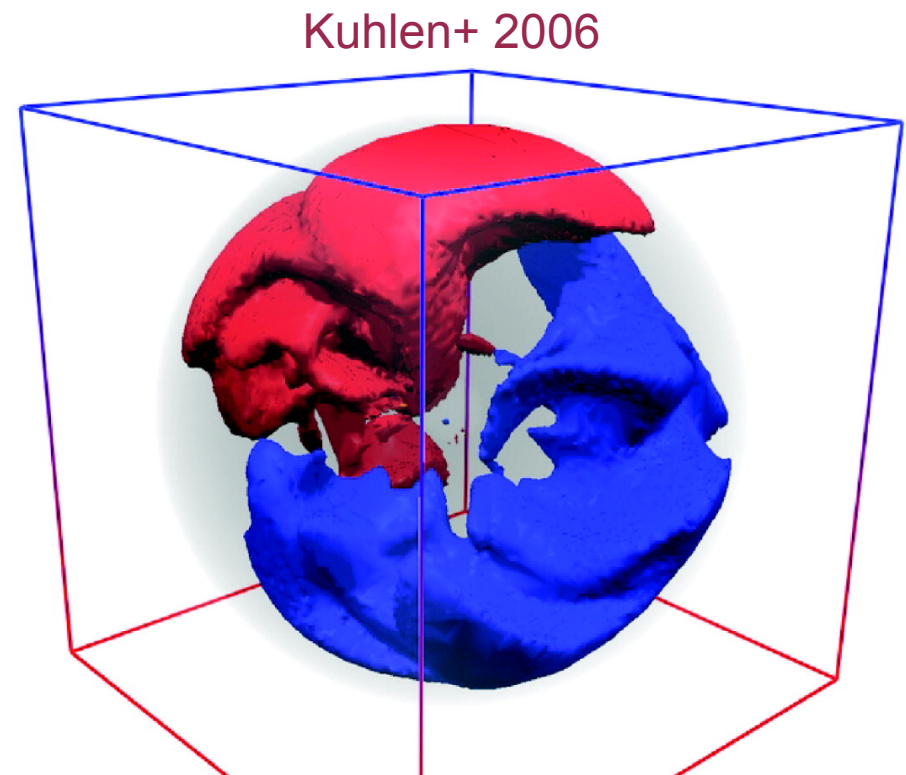
$$U_{c,\text{max}} \Delta t_{\text{CFL}} \quad 14$$

# Previous Simulations of Simmering



2d implicit hydro simulations; flows converged towards center suggesting central ignition

3d anelastic simulations of convection region; observed dipole flow that suggested off-center ignition



# Maestro

Nonaka+ 2011

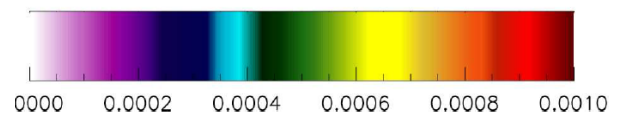
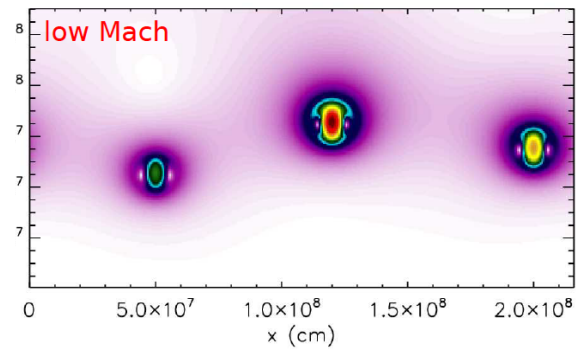
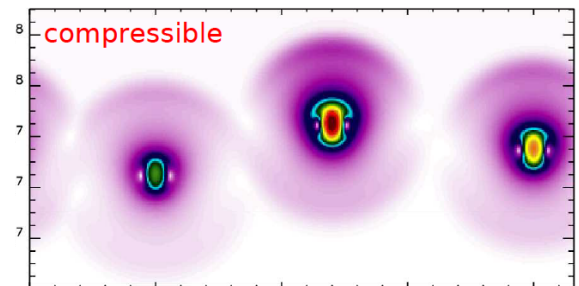
- Finite volume, AMR, low Mach hydro code that filters acoustic waves
- Retains important compressible effects from burning, diffusion, stratification
- Average HSE background state

$$\frac{|\pi|}{p_0} = \mathcal{O}(M^2)$$

$$p(x, t) = p_0(r, t) + \pi(x, t)$$

$$\nabla p_0 = -\rho_0 g$$

$$\Delta t_{\text{CFL}} \lesssim \frac{\Delta x}{U}$$





# Maestro

Nonaka+ 2011

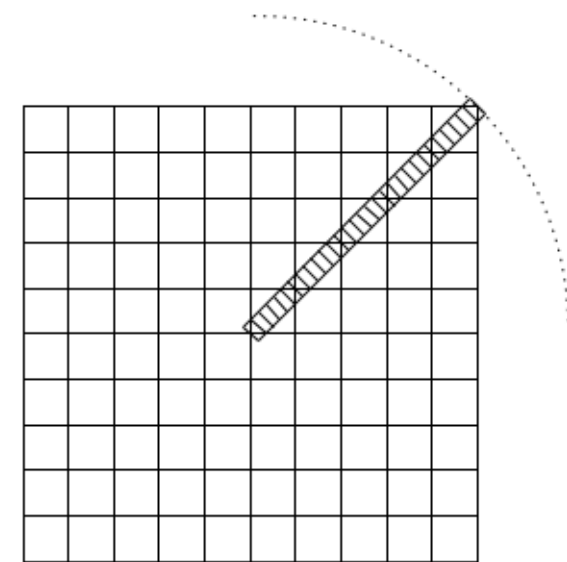
$$\frac{\partial (\rho X_k)}{\partial t} = -\nabla \cdot ({}_k \mathbf{U}) + \rho \dot{\omega}$$

$$\frac{\partial \mathbf{U}}{\partial t} = -\mathbf{U} \cdot \nabla \mathbf{U} - \frac{1}{\rho} \nabla \pi - \frac{\rho - \rho_0}{\rho} g \mathbf{e}_r$$

$$\frac{\partial (\rho h)}{\partial t} = -\nabla \cdot (\rho h \mathbf{U}) + \frac{Dp_0}{Dt} + \rho H_{\text{nuc}} + \nabla \cdot (\kappa \nabla T)$$

$$\nabla \cdot (\beta_0 \mathbf{U}) = \beta_0 \left( S - \frac{1}{\Gamma_1 p_0} \frac{\partial p_0}{\partial t} \right)$$

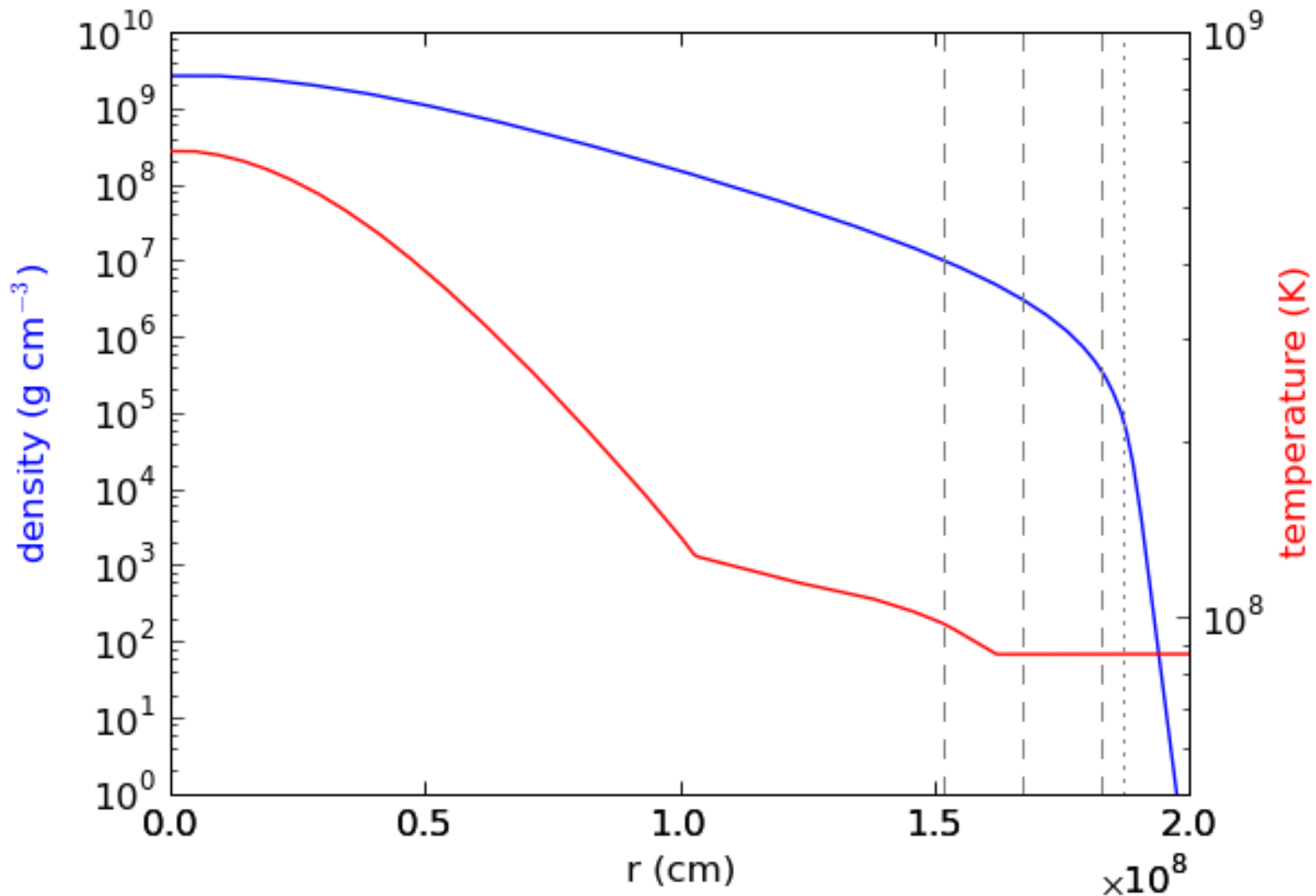
$$\beta_0(r, t) = \rho_0(r, t) \exp \left( \int_0^r \frac{1}{\Gamma_1 p_0} \frac{\partial p_0}{\partial r'} dr' \right)$$



- Advection using 2<sup>nd</sup> order Godunov
- Reactions using Strang splitting (Stiff ODEs)
- Diffusion semi-implicit (multigrid)
- Divergence constraint – elliptic solve (multigrid)

# Initial Conditions

Zingale+ 2011

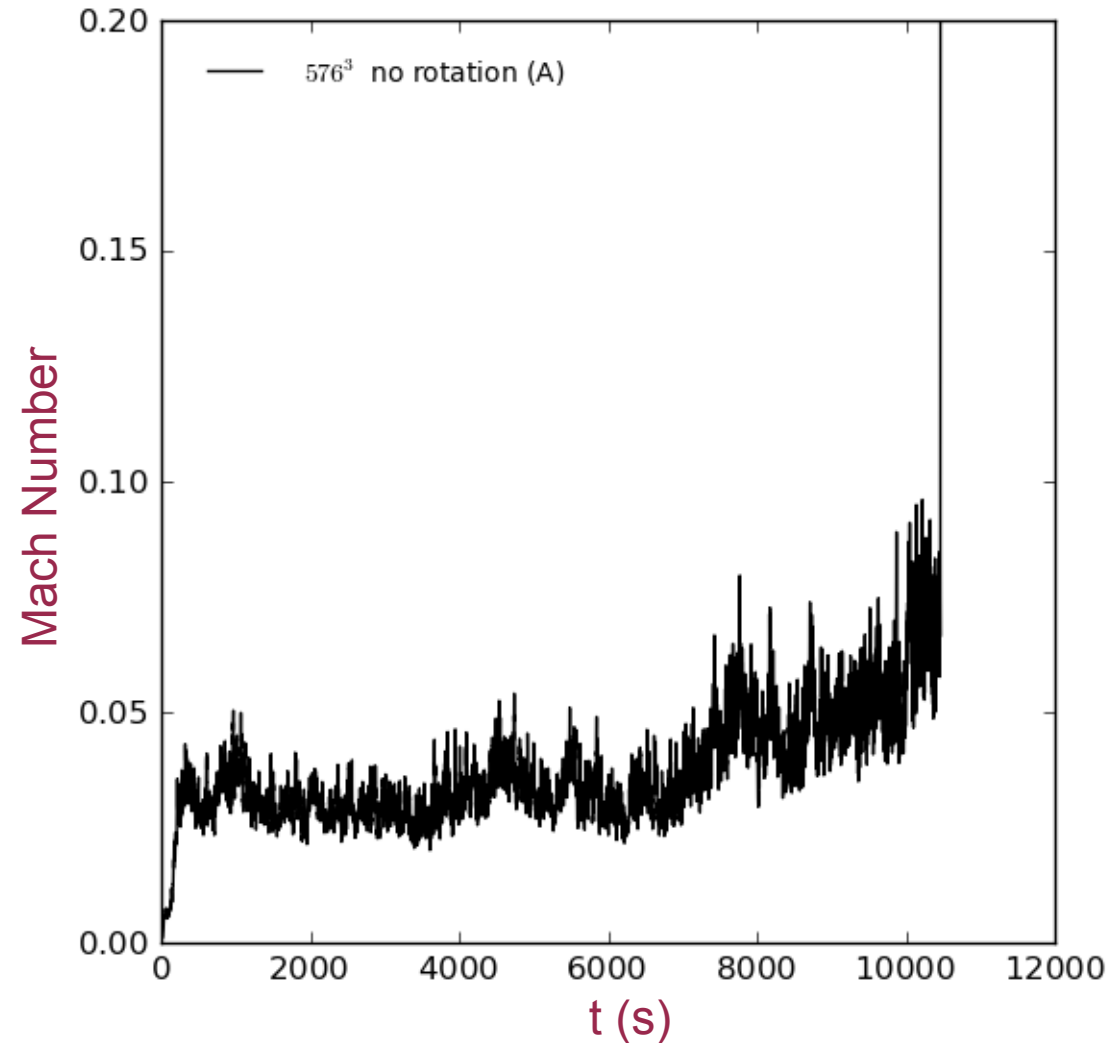
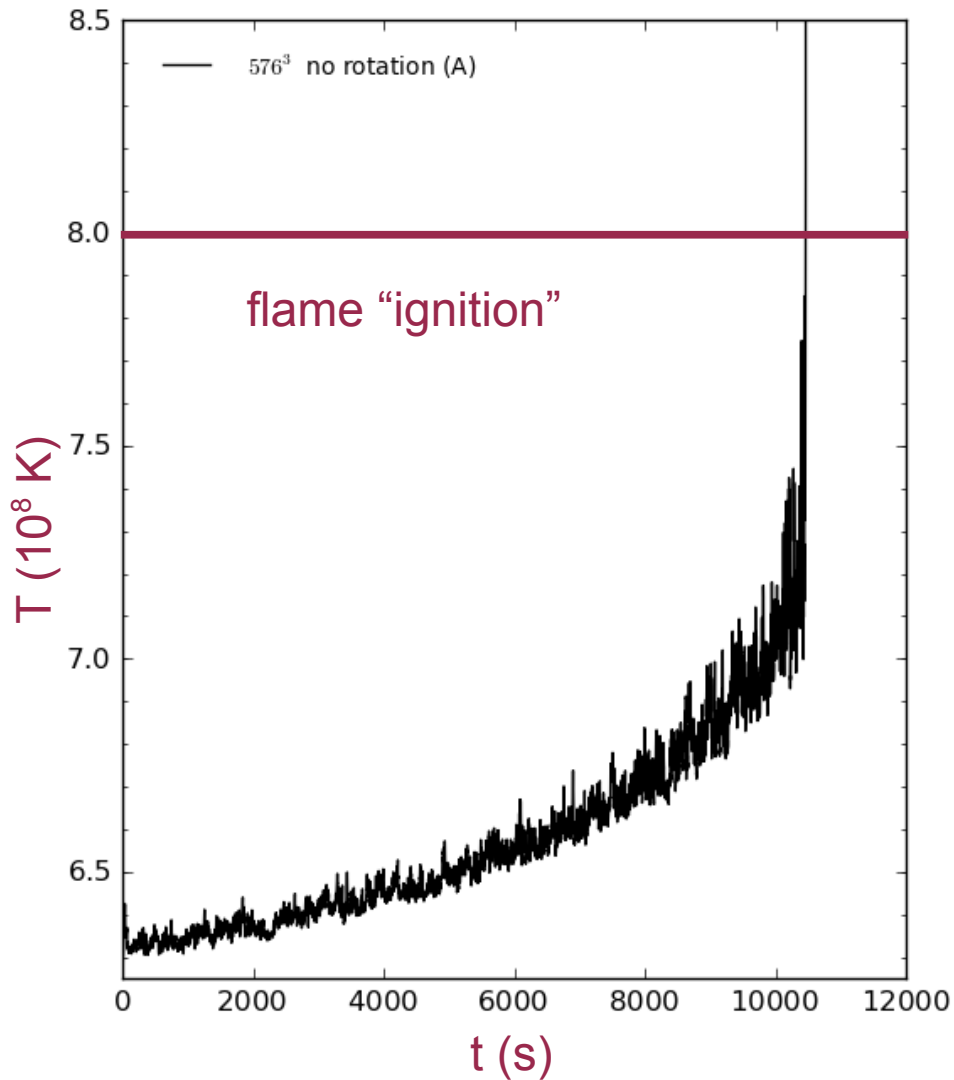


Based on Kepler model

# Simmering to Ignition

Zingale+ 2011

8.7 km / zone



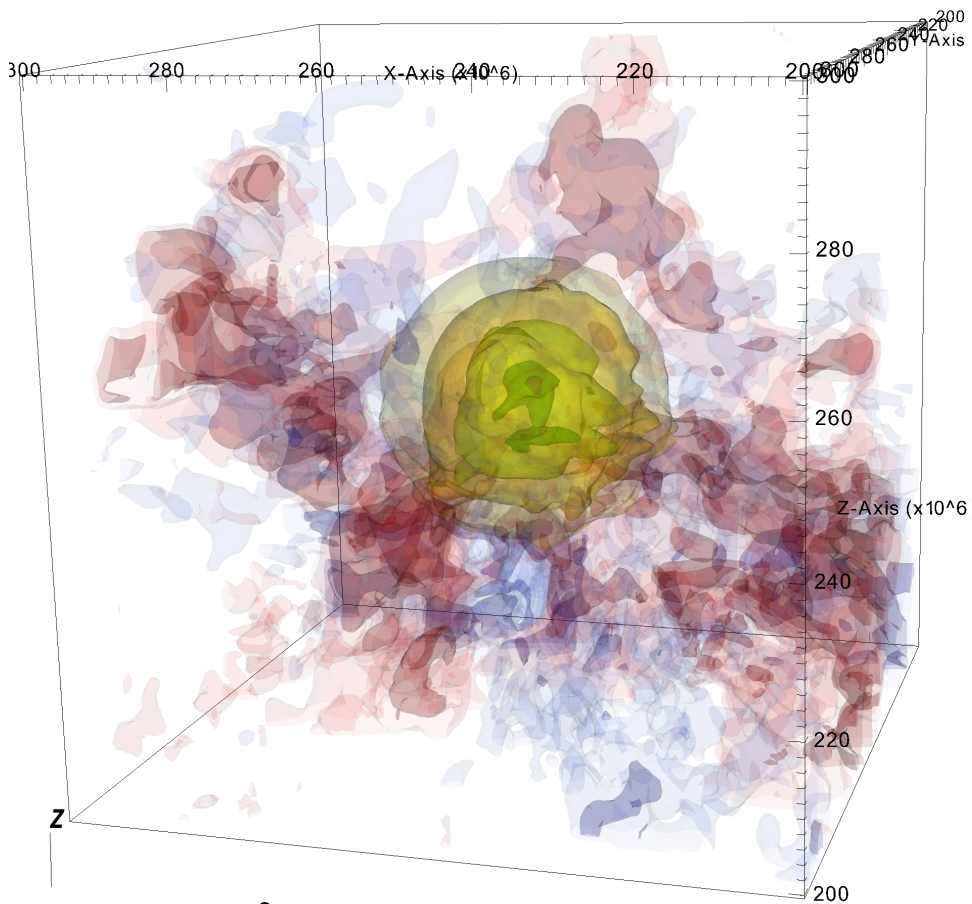
# Simmering to Ignition

Zingale+ 2011

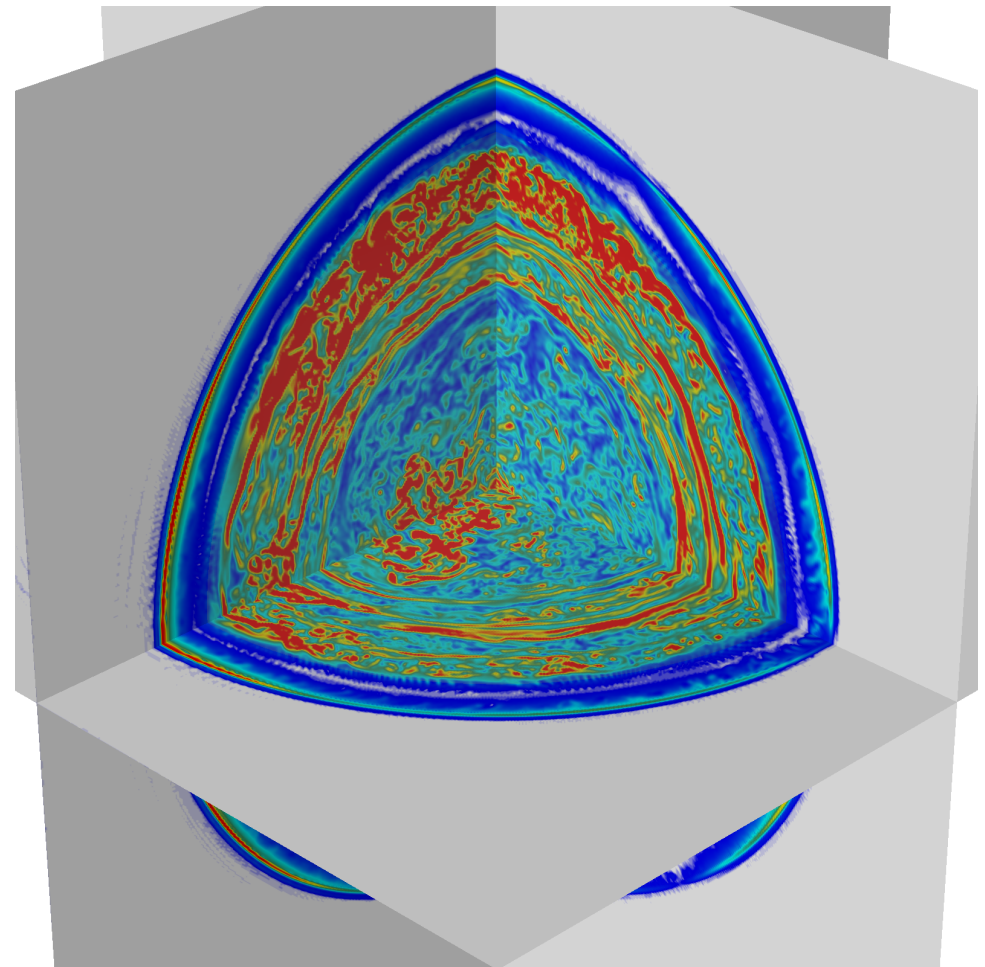
EGR – yellow/green/purple  
Rad. Vel – red/blue

8.7 km / zone

Mag. vorticity



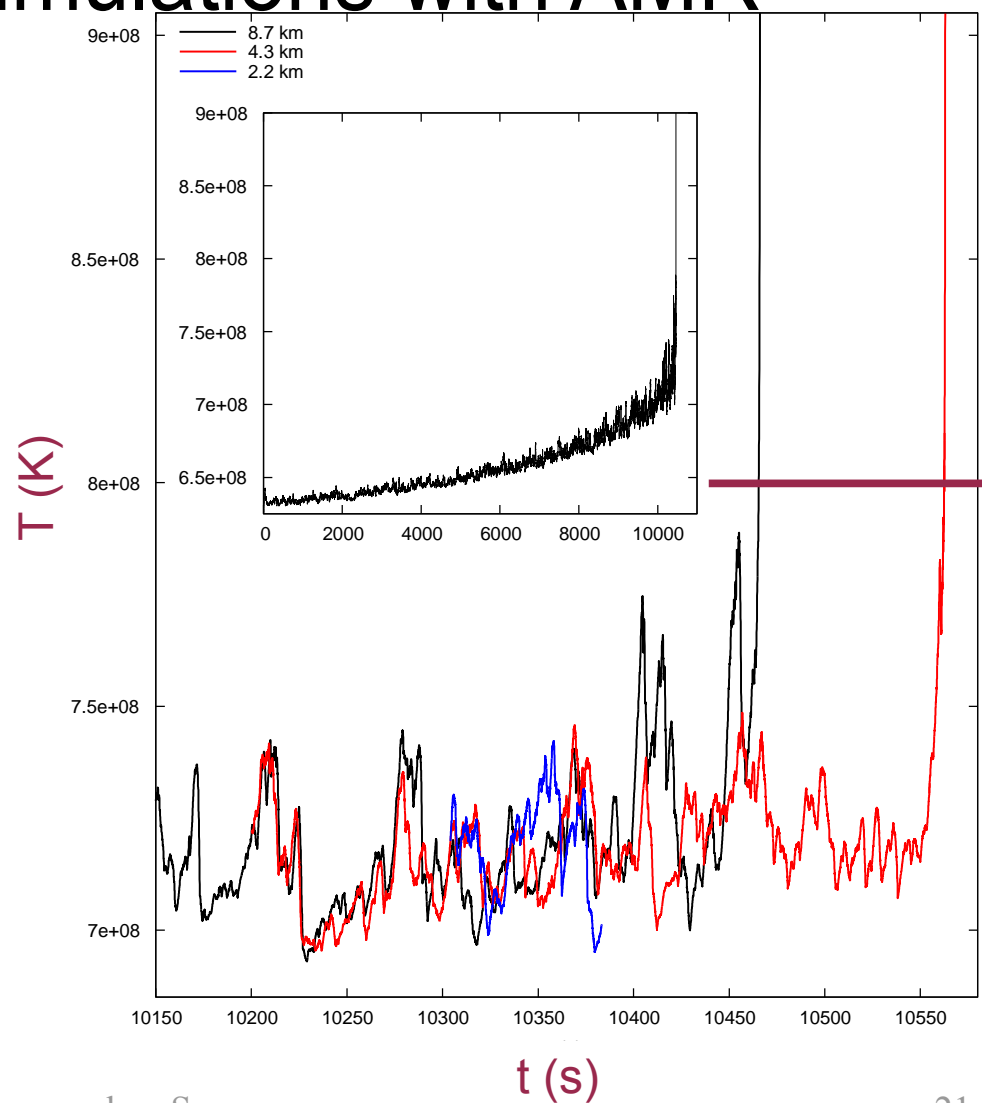
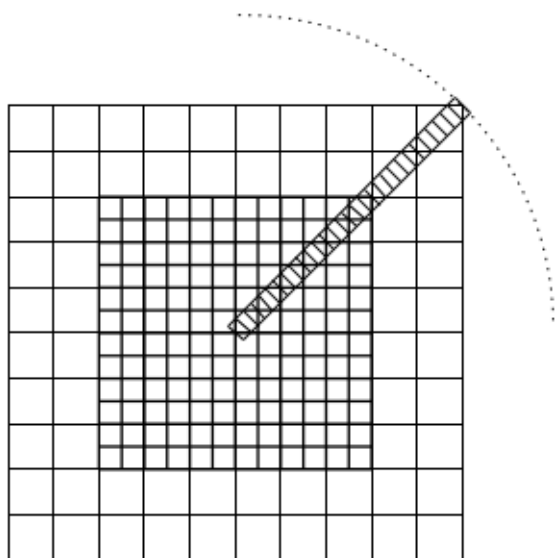
Inner 1000<sup>3</sup> km



# Simmering to Ignition

Nonaka+ 2012

- Added refinement to simulations with AMR
- Up to effective  $2304^3$  (2.1 km / zone)

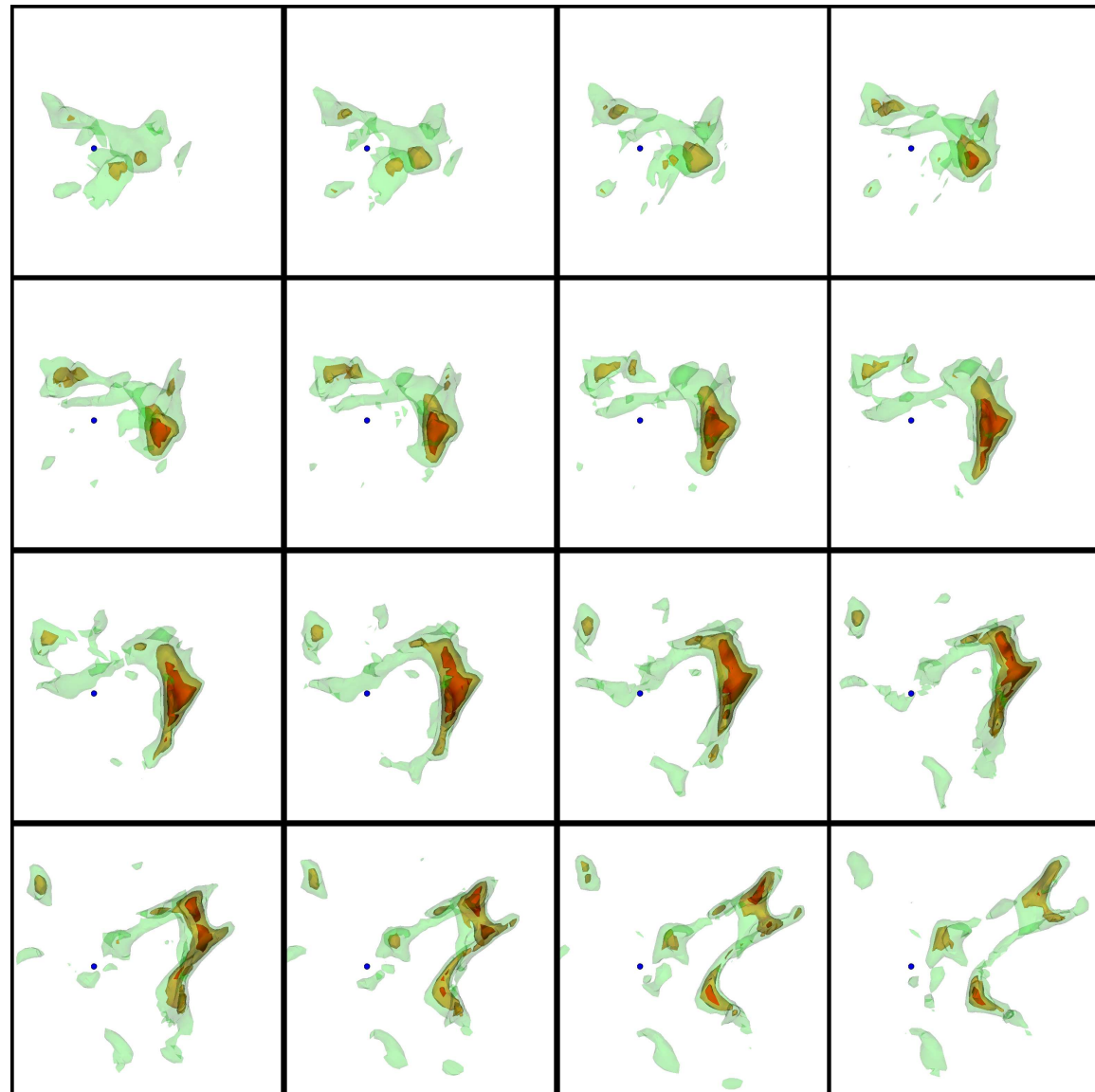


# Simmering to Ignition

Nonaka+ 2012, 4.3 km / zone

Green:  $T_8 = 7.5$   
Yellow:  $T_8 = 7.7$   
Orange:  $T_8 = 7.9$

Ignition localized  
and off-center!

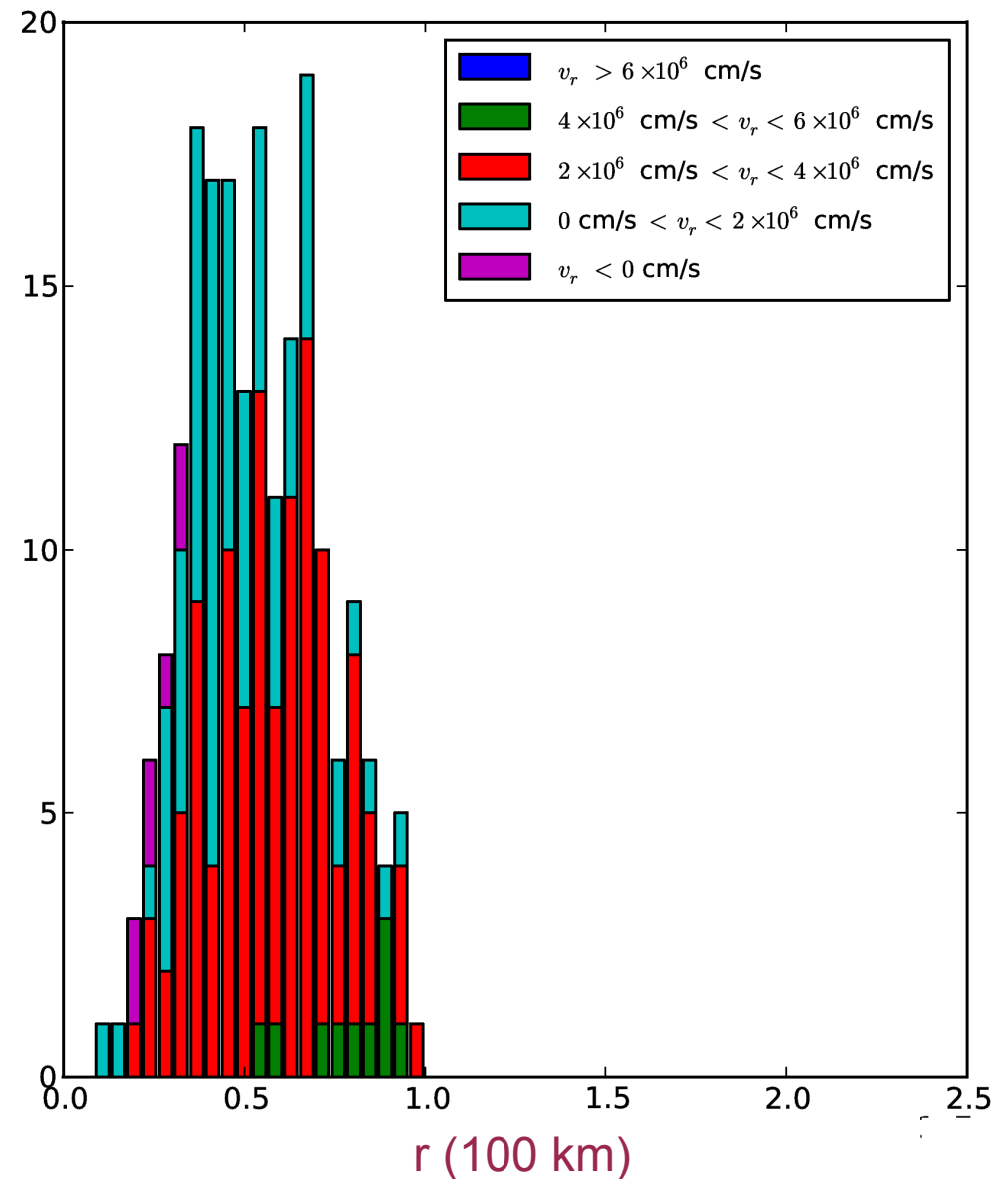


# Simmering to Ignition

Zingale+ 2011, Nonaka+ 2013

Ignition occurs in region of outflow!

Ignition localized and off-center!



# Castro

Almgren+ 2010,(Zhang+ 2011, 2013)

- Finite volume, AMR compressible (rad)-hydro code
- Sub-cycling in time
- Multigrid solvers for gravity/diffusion
- Same underlying data structures as Maestro (BoxLib)



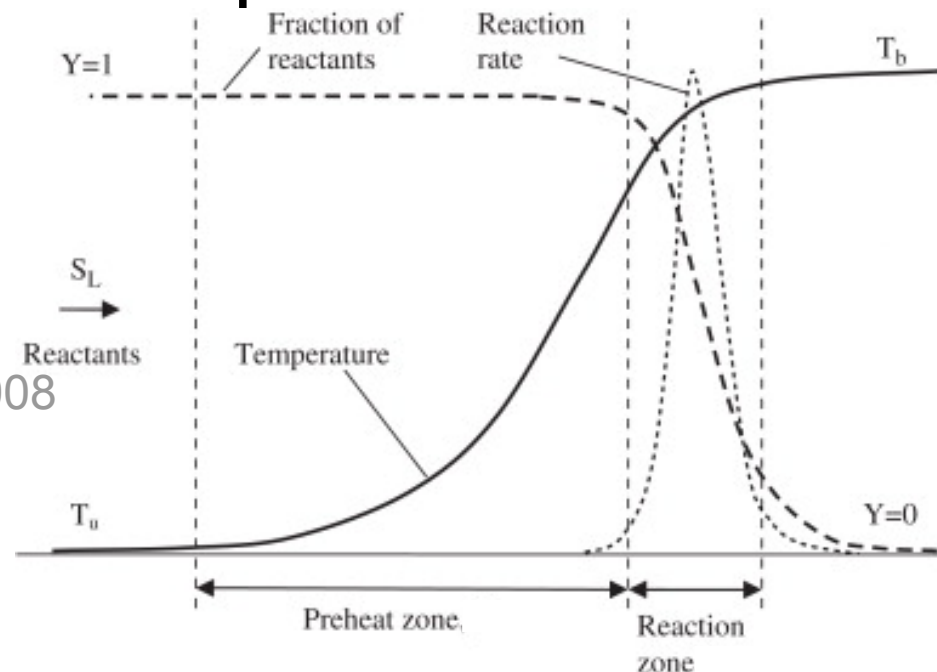
# Astrophysical Flames

- Flame thickness at ignition  $\delta \sim 10^{-2}$  cm
- Radius of star  $R_{\text{WD}} \sim 10^8$  cm
- Thermal diffusion much more important than species diffusion  $Le \gg 1$

Laminar flame

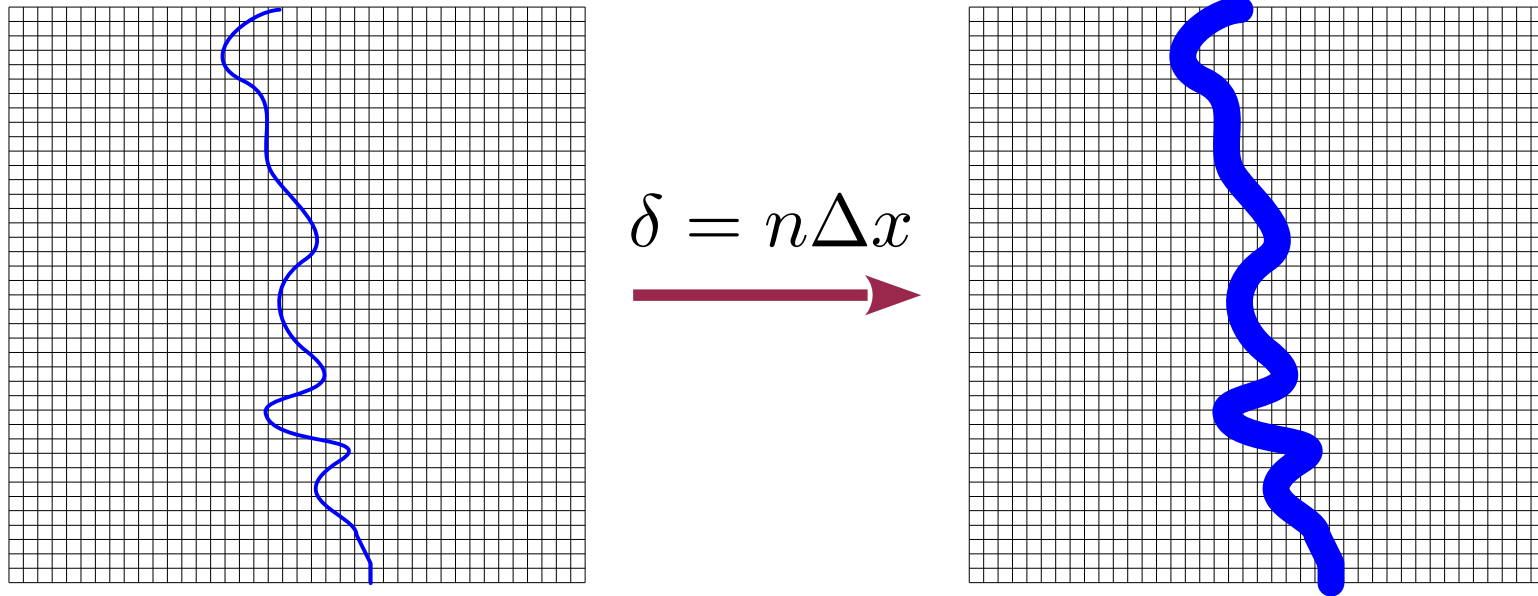
after

Ciccarelli & Dorofeev 2008



Turbulence highly complicates the burning!

# Thickened Flame



Steady state :  $\tau_{\text{diff}} = \tau_{\text{burn}}, \quad v_f = \frac{\delta}{\tau_{\text{diff}}}$

Given a flame speed and EGR, find a consistent diffusion coefficient

$$\kappa \simeq \frac{(\Delta x)^2}{\tau_{\text{diff}}} \simeq \frac{(v_f \tau_{\text{burn}} / n)^2}{\tau_{\text{burn}}} \simeq \tau_{\text{burn}} \left( \frac{v_f}{n} \right)^2$$

# Thickened Flame

Ma+ 2013

- Burning timescale determined by table interpolation of off-line large reaction networks

Log $\rho$ (g cm <sup>-3</sup> )	$T_{9f}$ (10 <sup>9</sup> K)	$\rho_{7f}$ (10 <sup>7</sup> g cm <sup>-3</sup> )	$d\rho_7/d X_{12}$ (10 <sup>7</sup> g cm <sup>-3</sup> )	BE/A (MeV/nucleon)	$\bar{A}$
6.40	1.790	0.122	0.258	8.040	18.340
6.50	1.903	0.158	0.316	8.046	18.430
6.60	2.036	0.203	0.390	8.057	18.630

Log T	Log density	$Y_e$	X(He)	X(Si-Ca)	X(Fe group)	$\bar{A}$	BE/A	$dY_e/dt$
9.80	9.30	0.500	1.601(-2)	5.174(-2)	0.9322	35.29	8.55635	2.617(-1)
9.80	9.30	0.495	1.205(-2)	4.097(-2)	0.9469	40.79	8.60340	1.920(-1)
9.80	9.30	0.490	9.798(-3)	2.832(-2)	0.9618	44.58	8.63952	1.313(-1)

- Flame speed currently set to constant\*

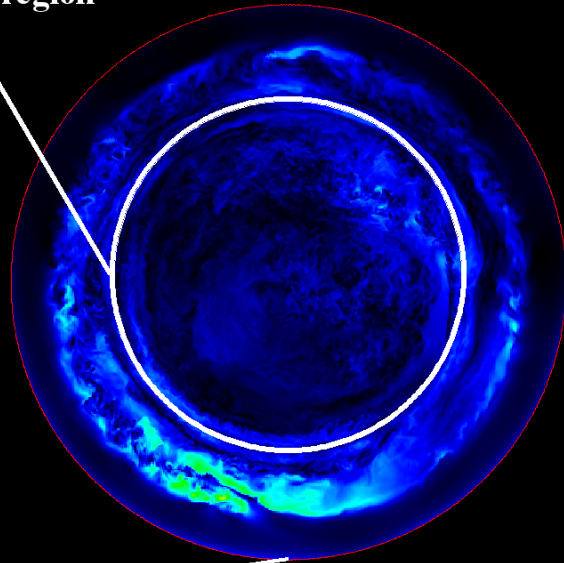
# Maestro to Castro

Malone+ 2013

Slice through MAESTRO results of magnitude of velocity

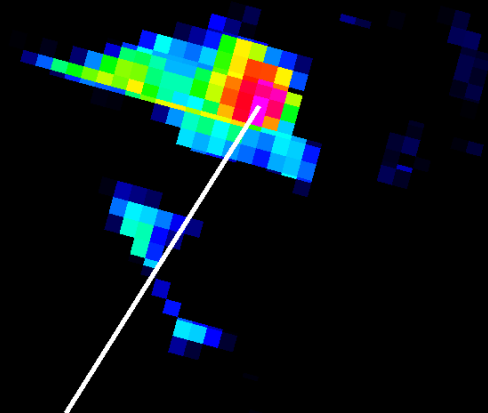
Convective region

Stellar surface



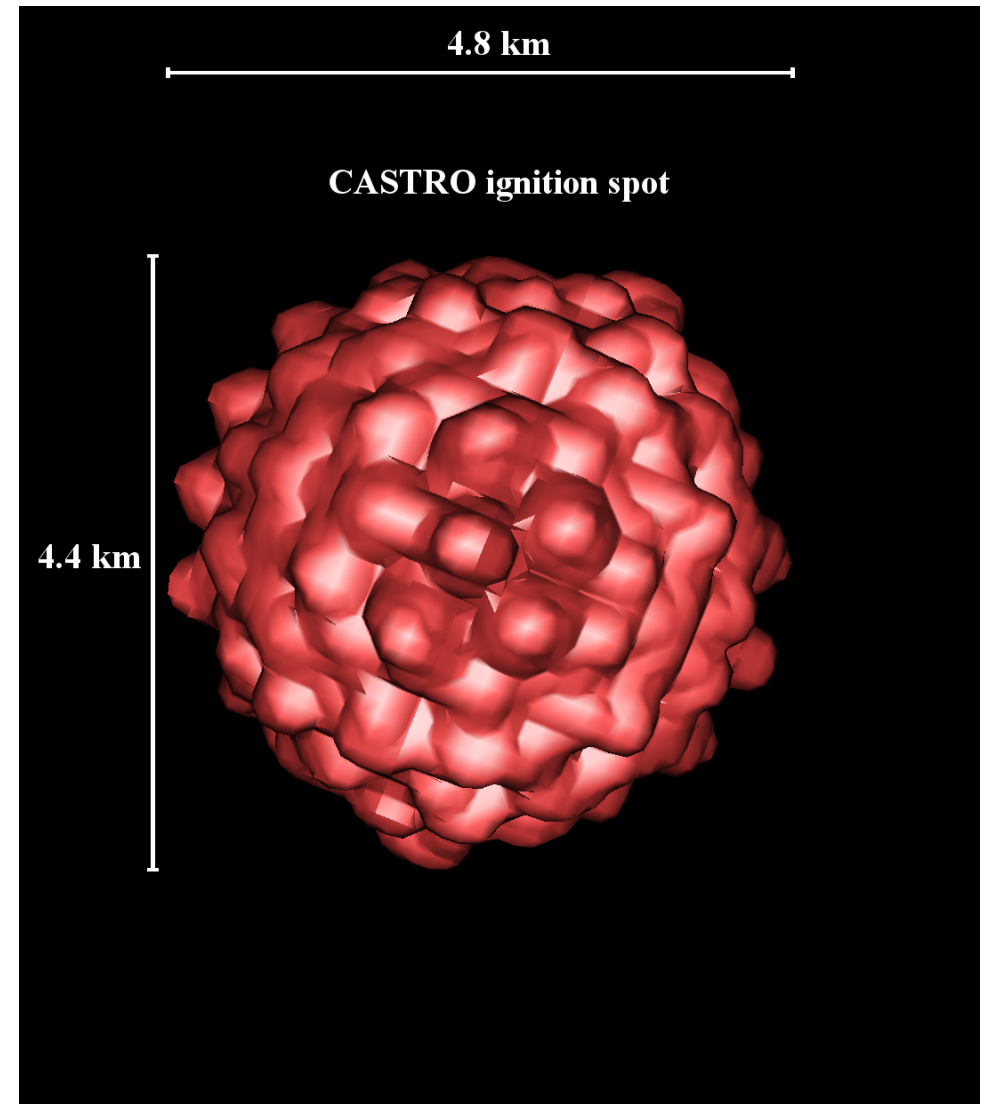
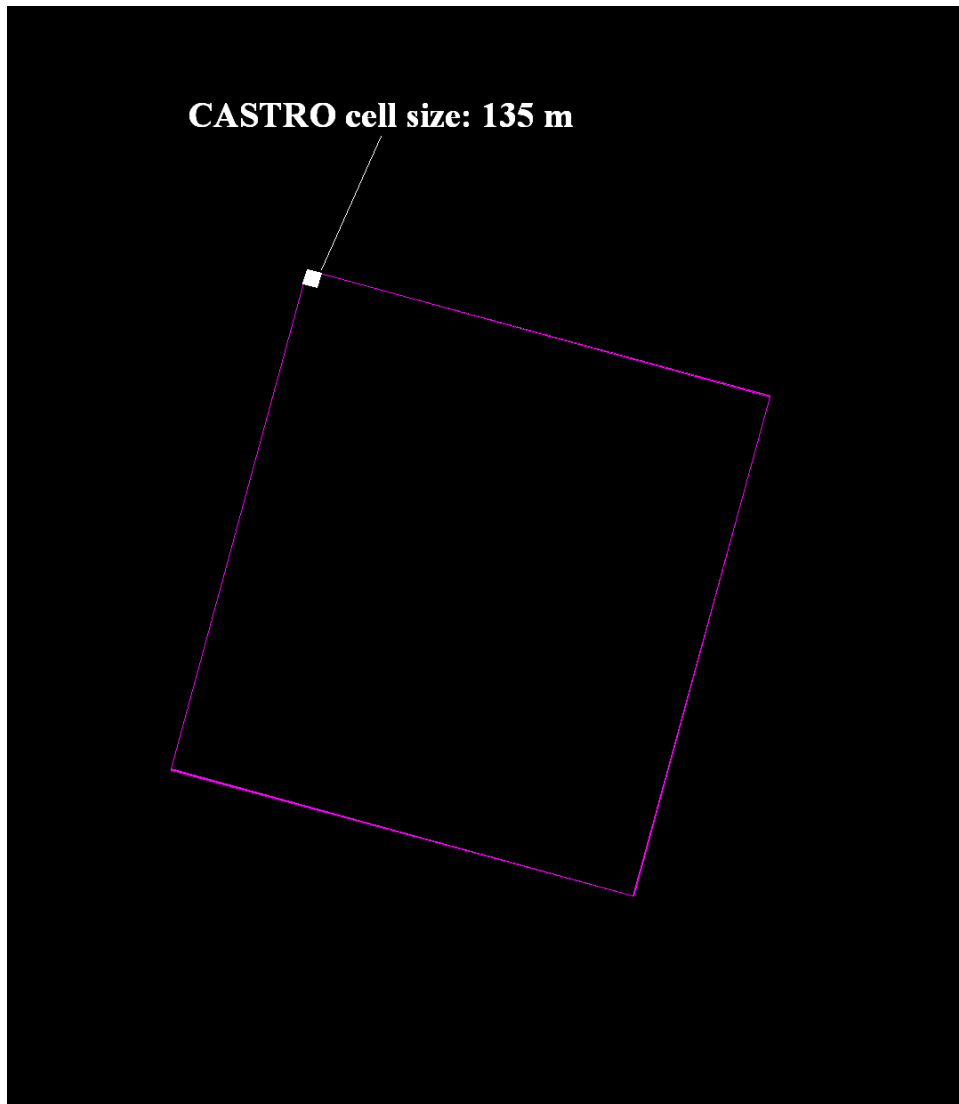
Zoom in on MAESTRO ignition point

Ignition zone:  $T \sim 8e8$  K



# Maestro to Castro

Malone+ 2013

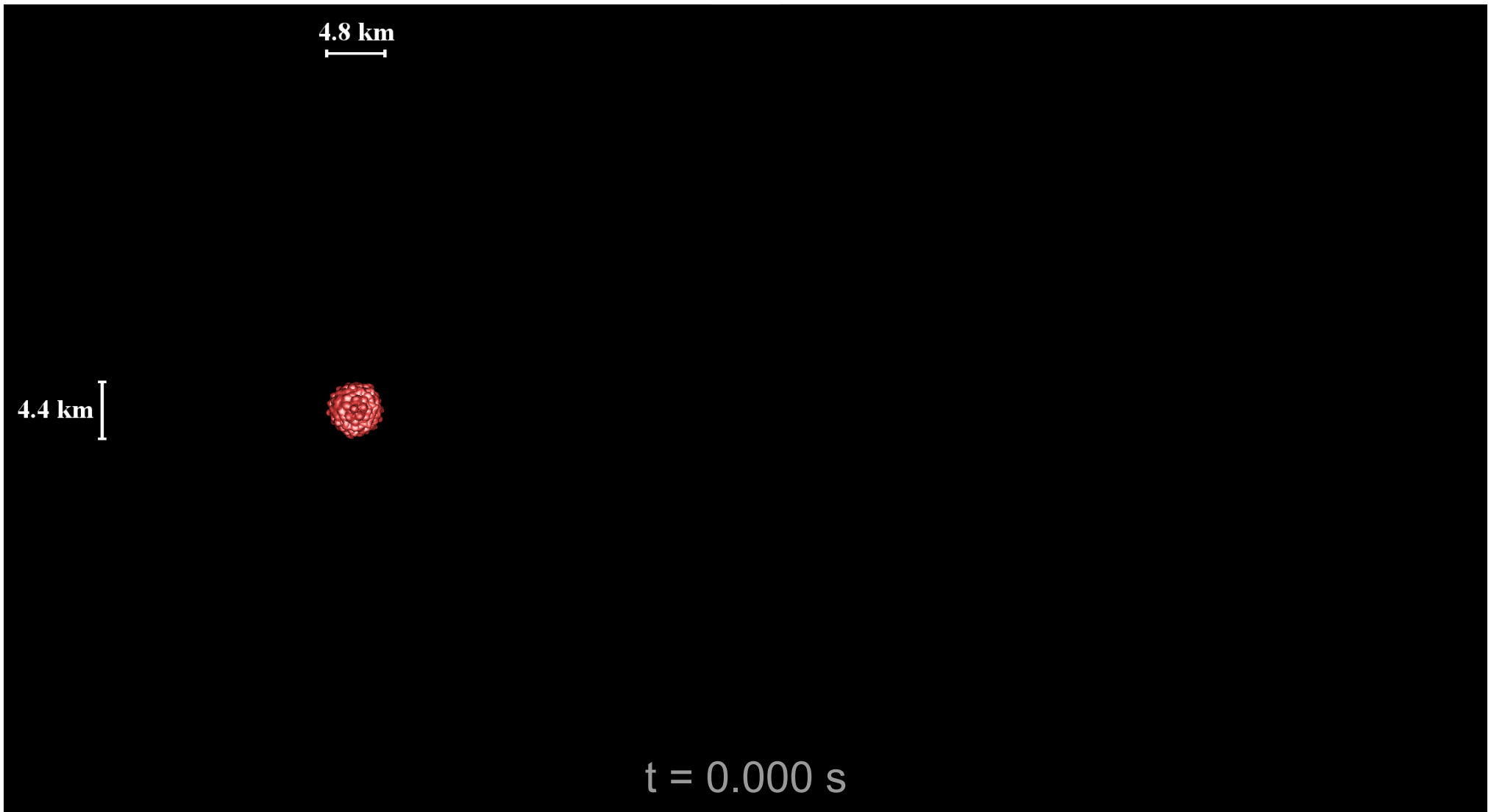


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$



# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

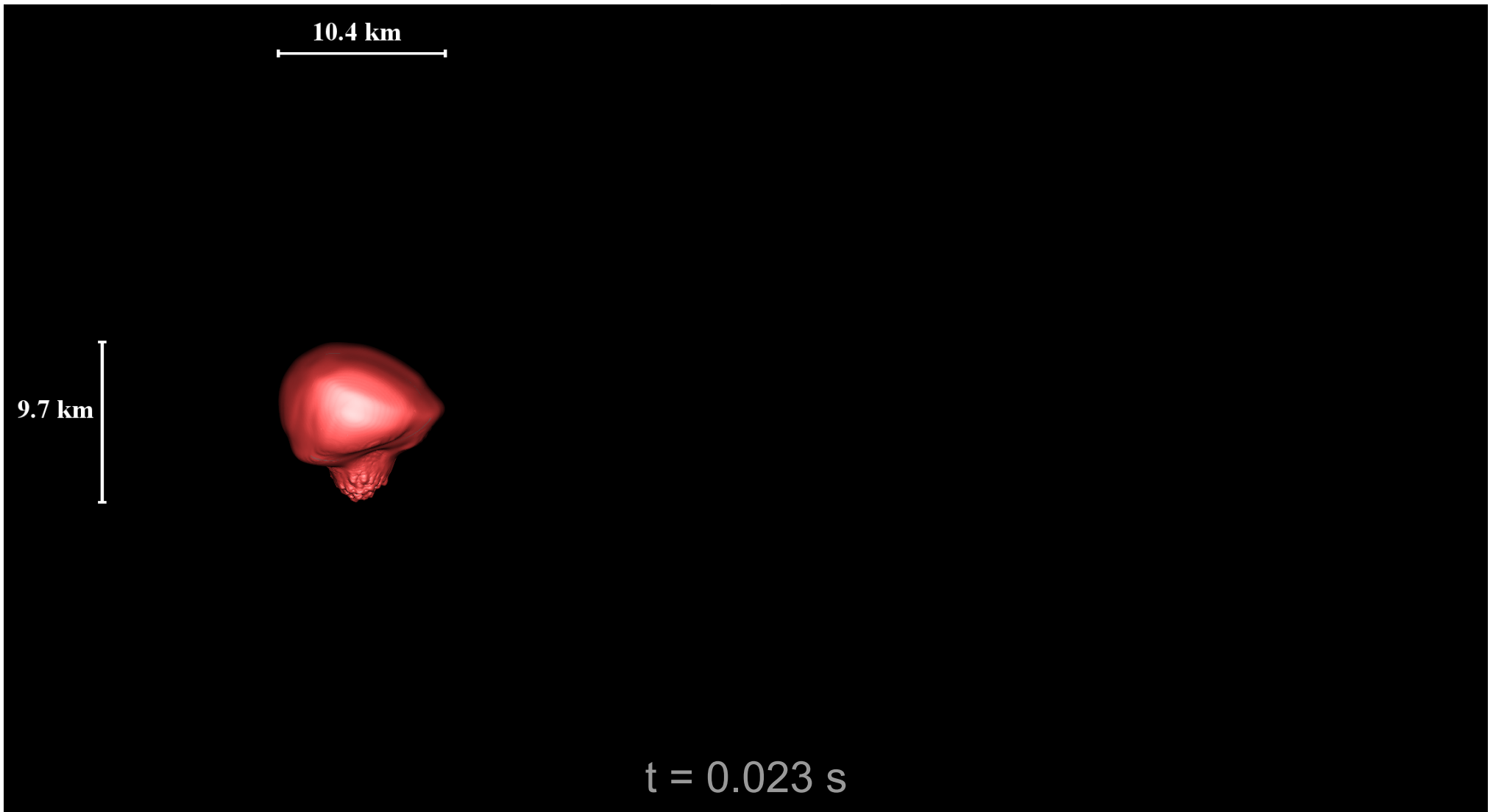


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$



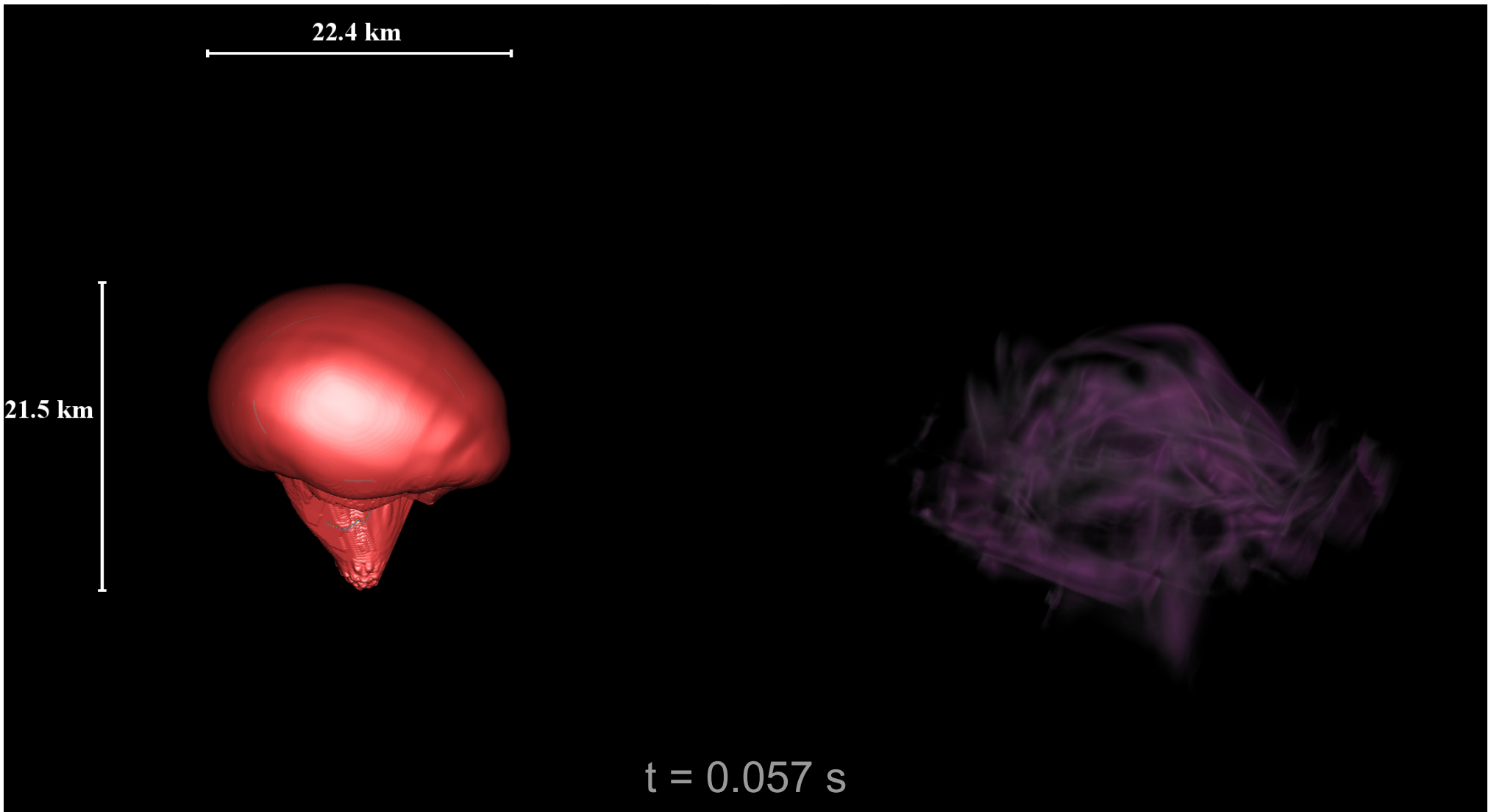


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

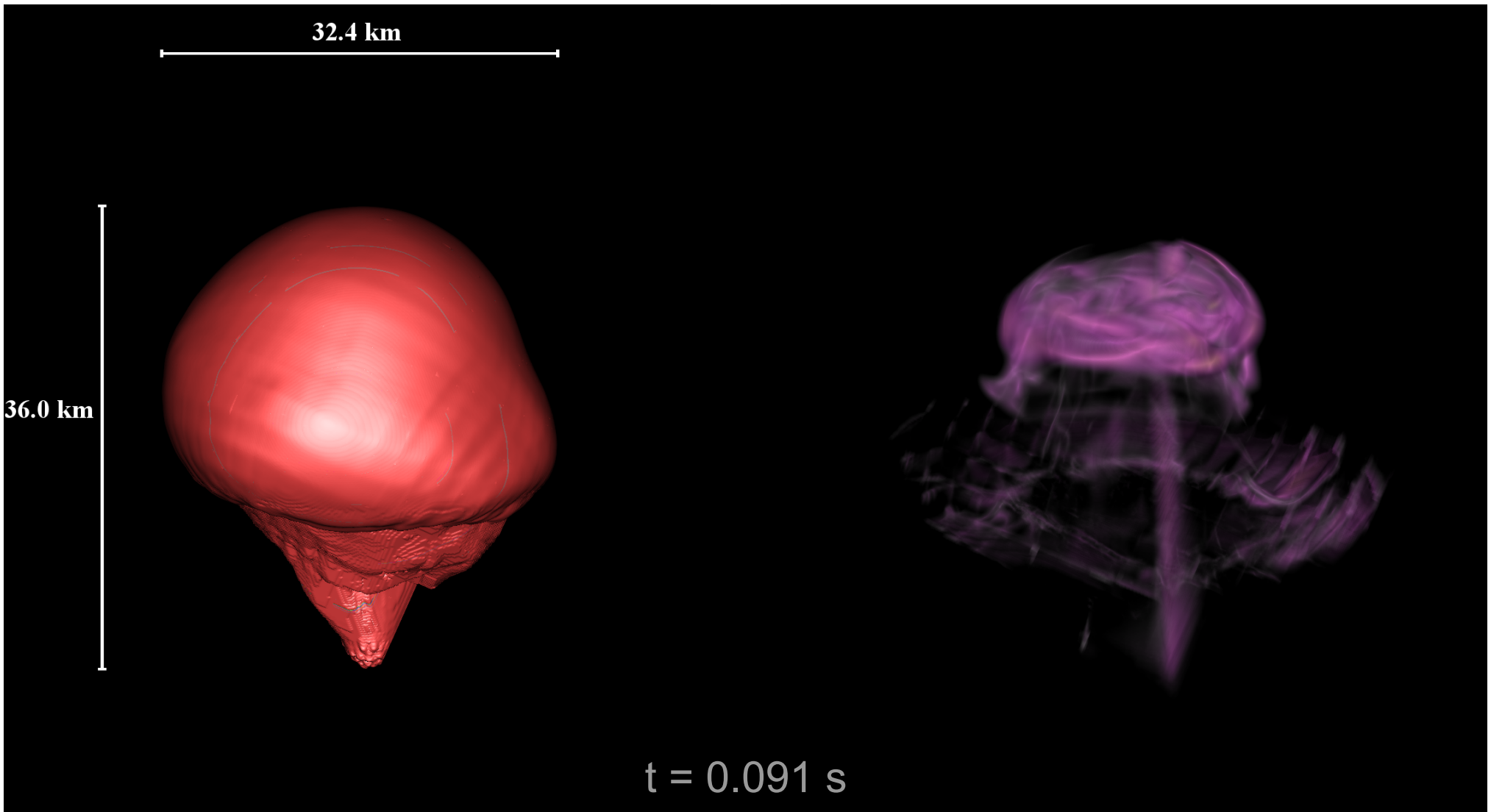


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

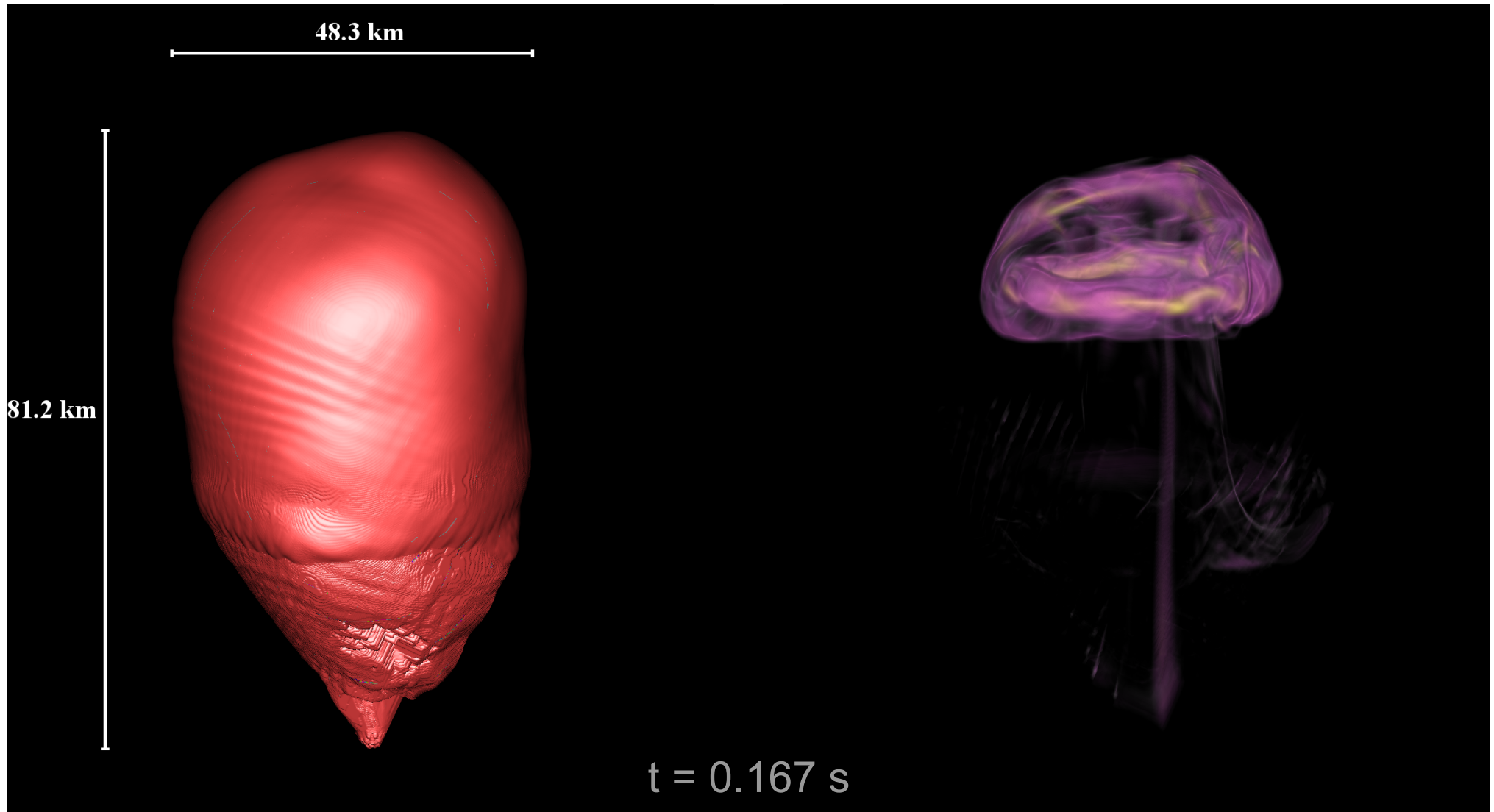


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

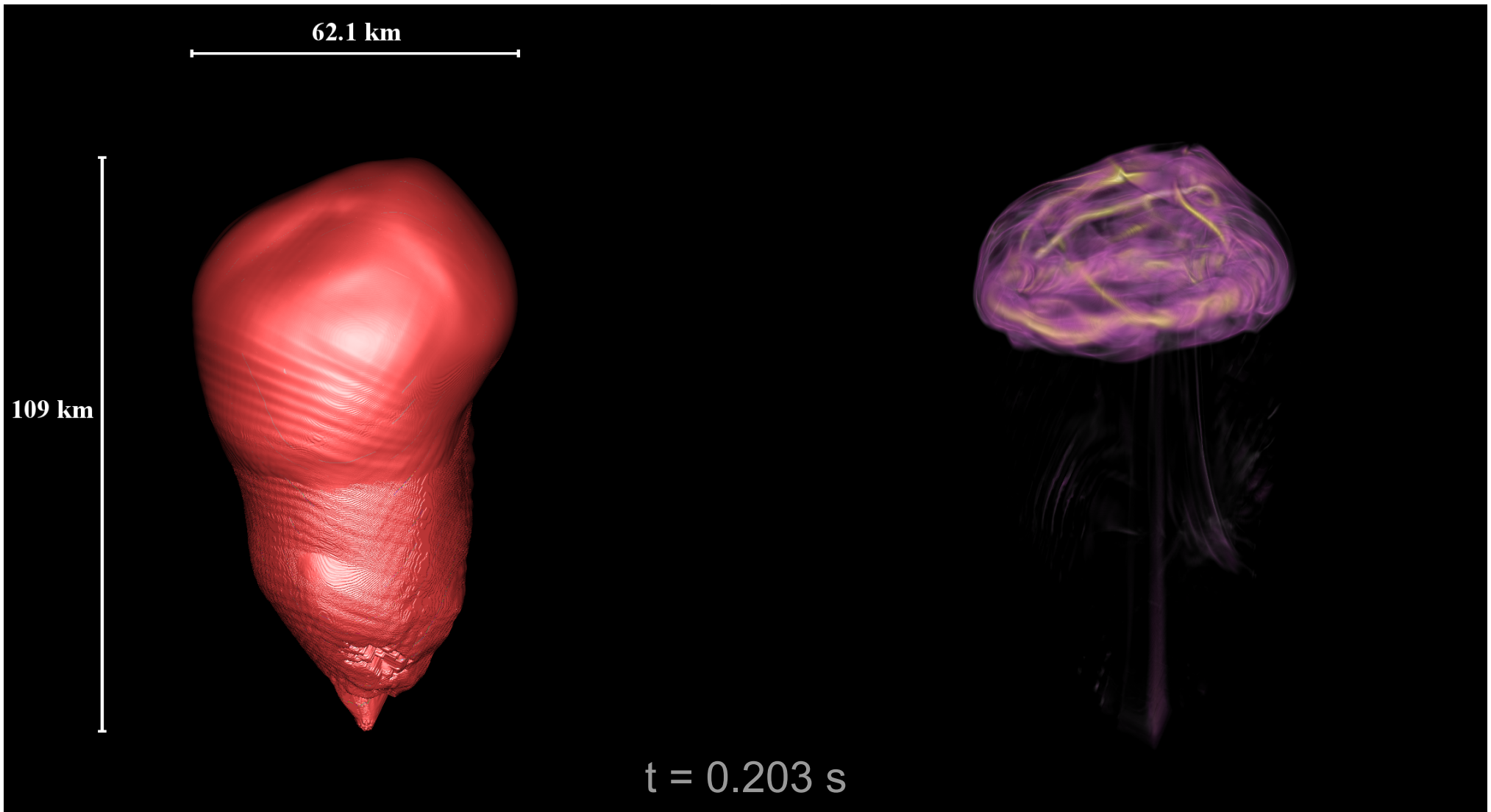


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

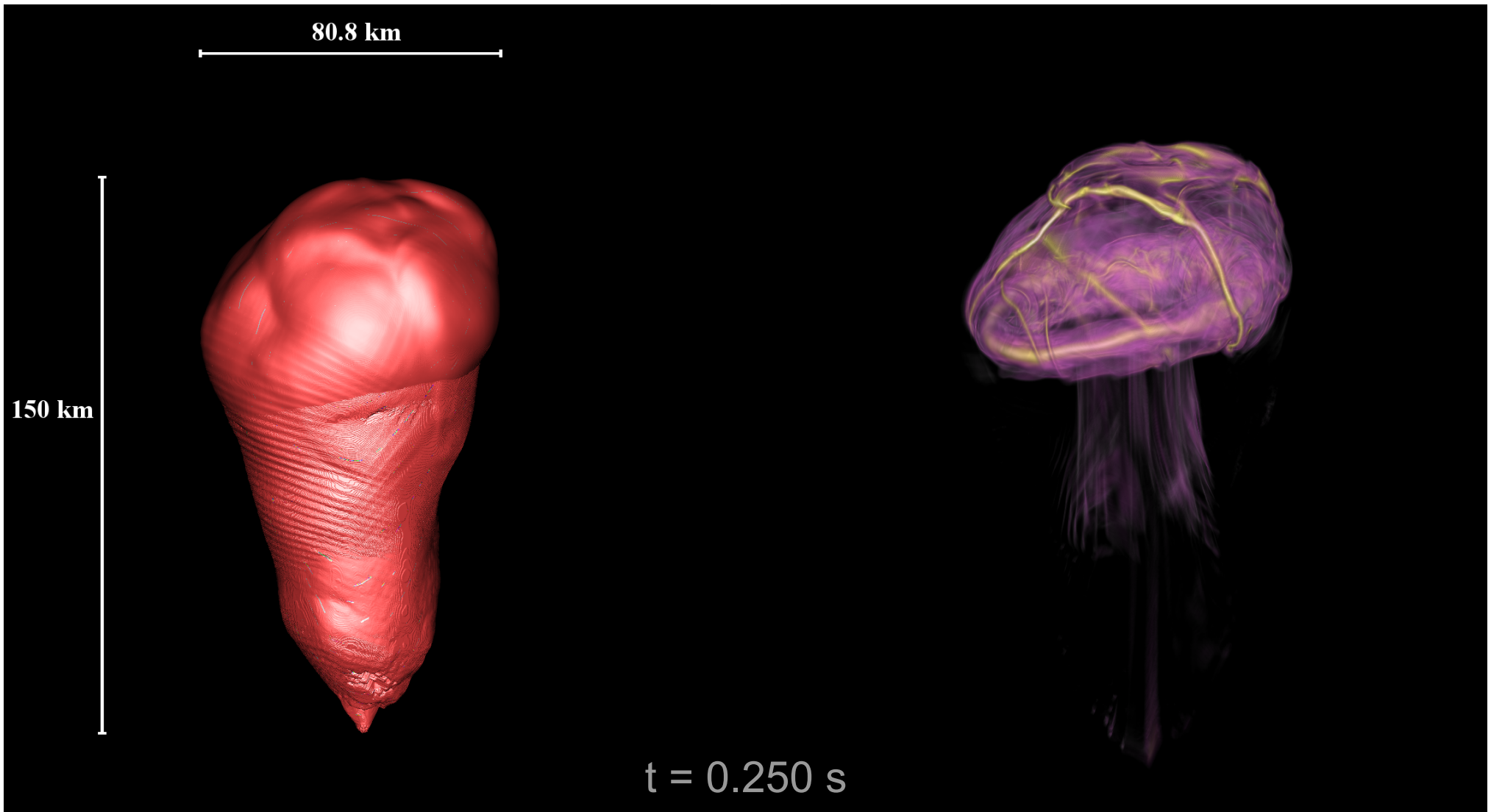


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

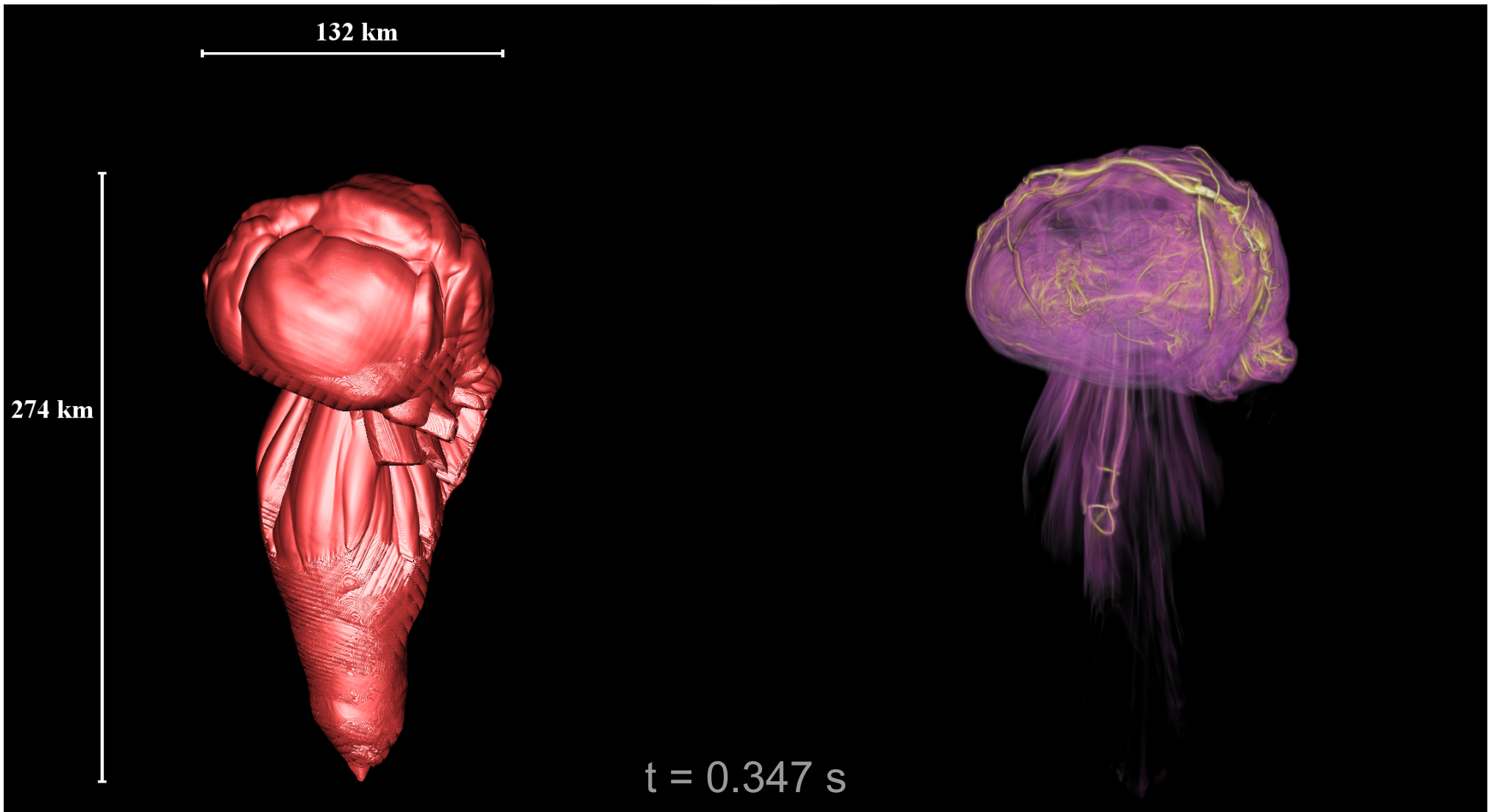


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

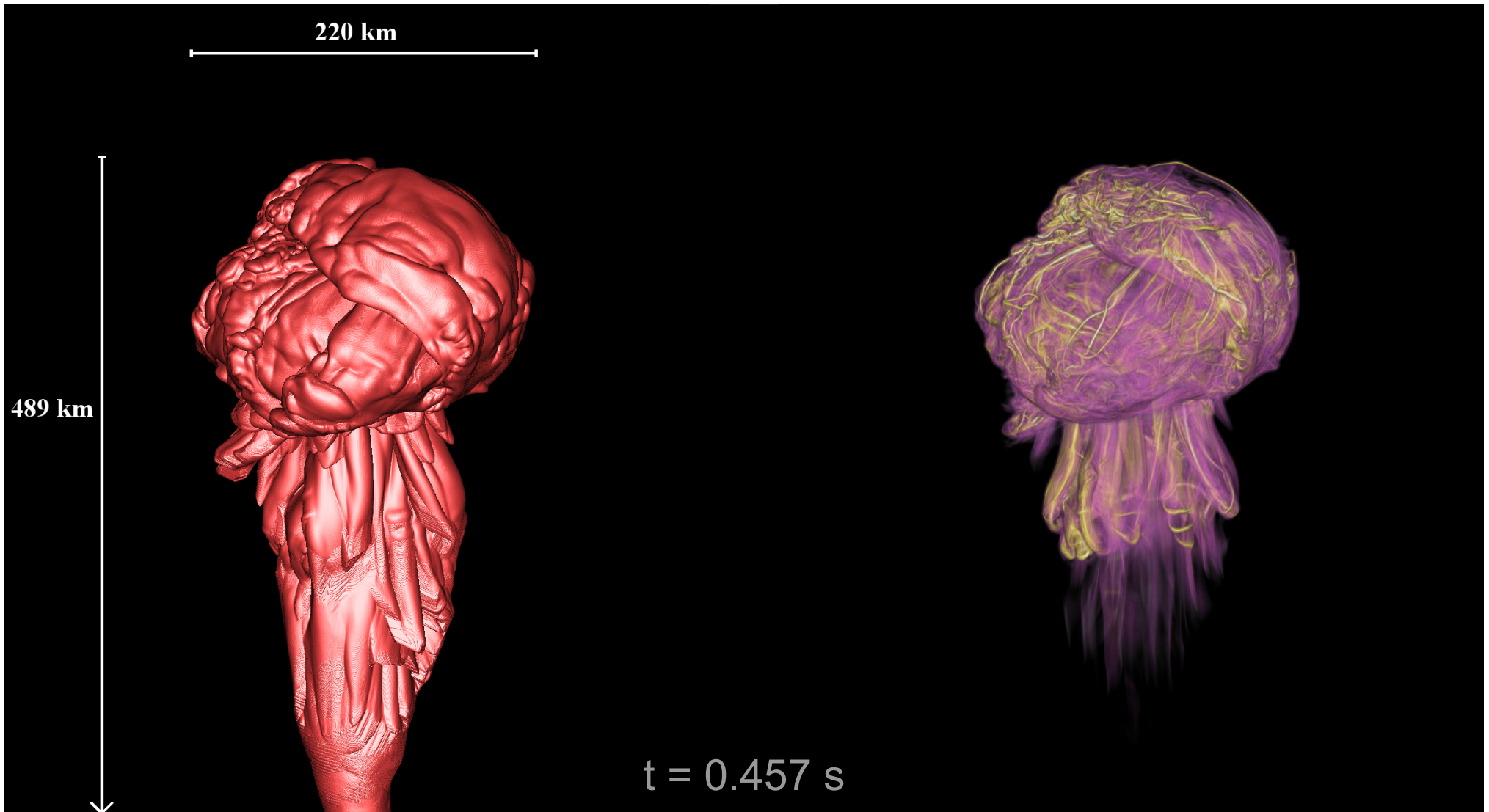


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

Malone+ 2013

$$|\nabla \times \mathbf{U}|$$

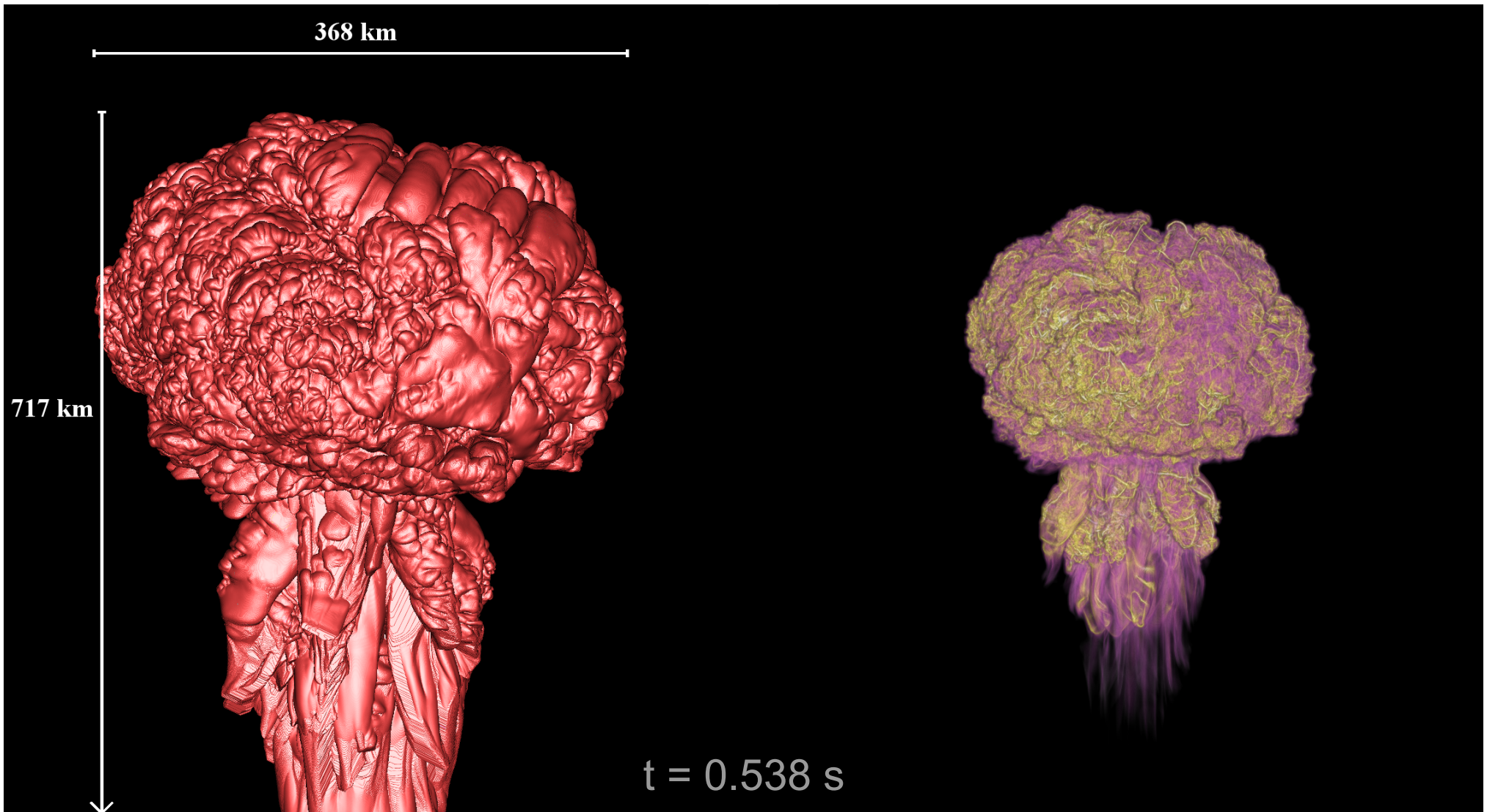


# Bubble Rise

$$X(^{12}\text{C}) = 0.49$$

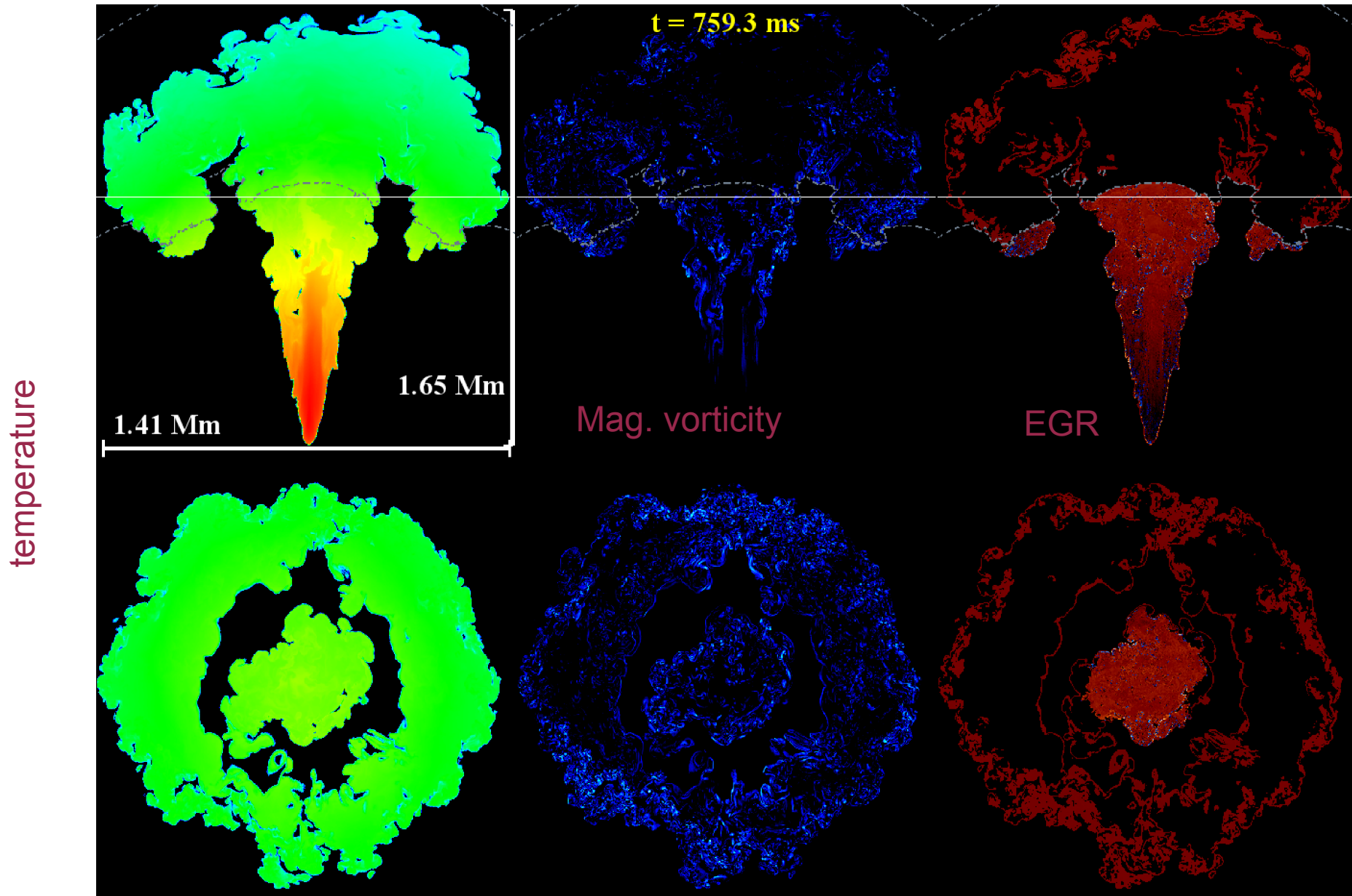
Malone+ 2013

$$|\nabla \times \mathbf{U}|$$





# Slices – Interesting Burning

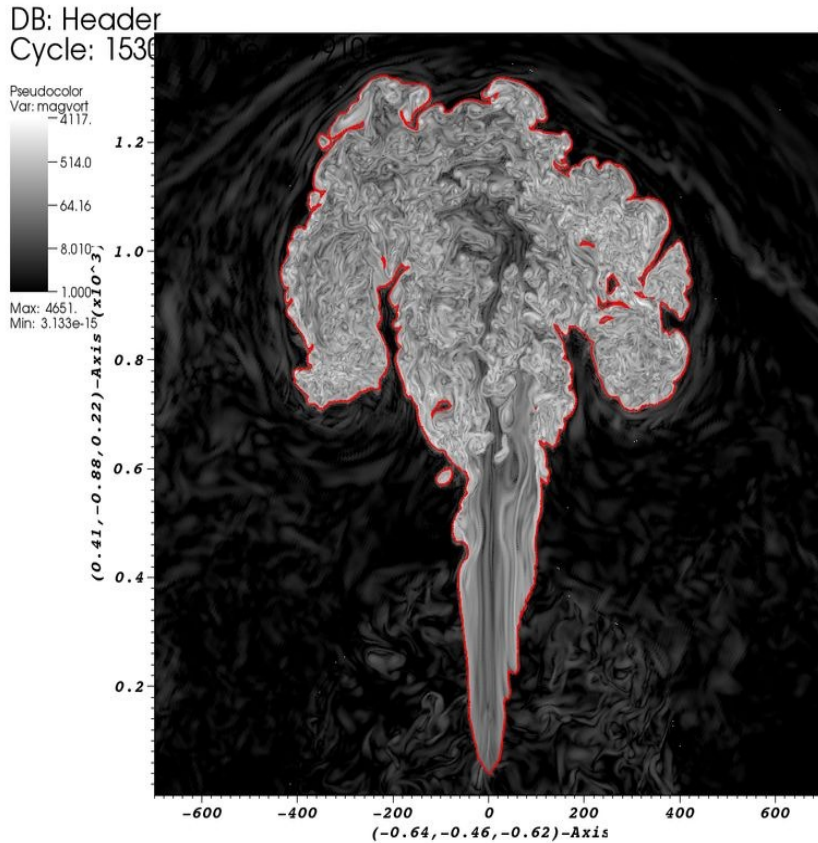


# Turbulence Only In Ash?

Mag. vorticity

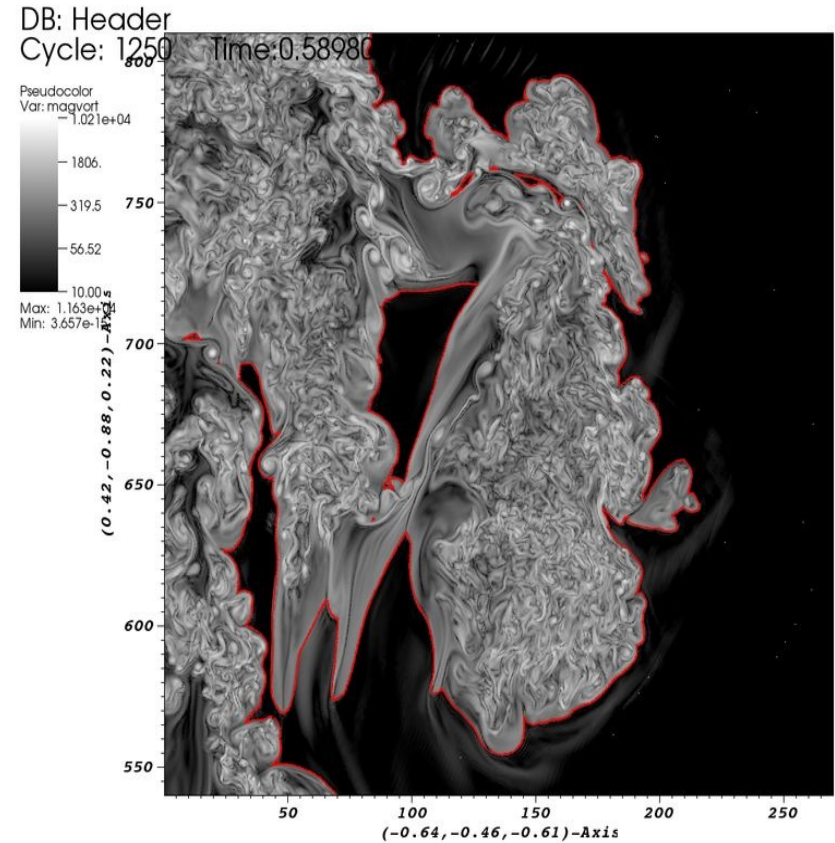
Malone+ 2013

Mag. vorticity



user: cmalone  
Fri May 25 13:37:14 2012

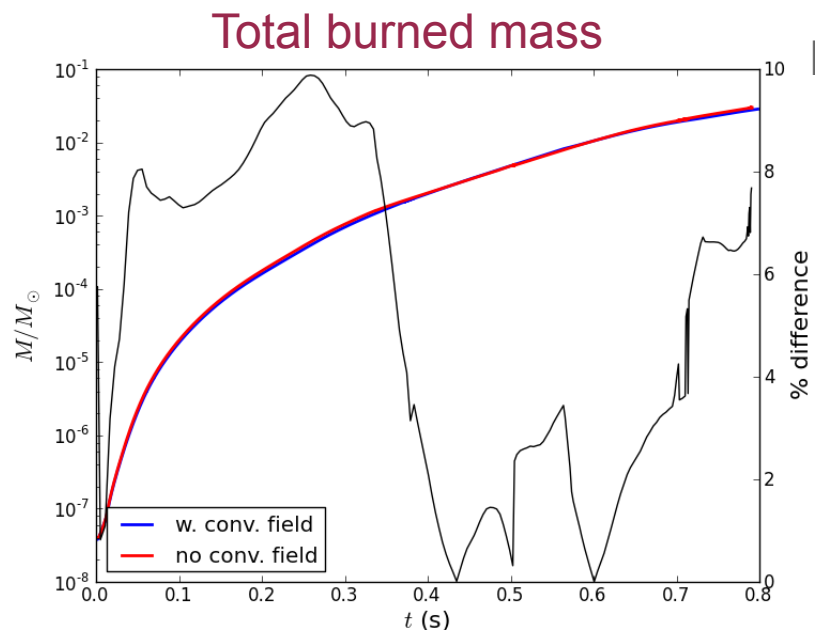
Plowing through convective field



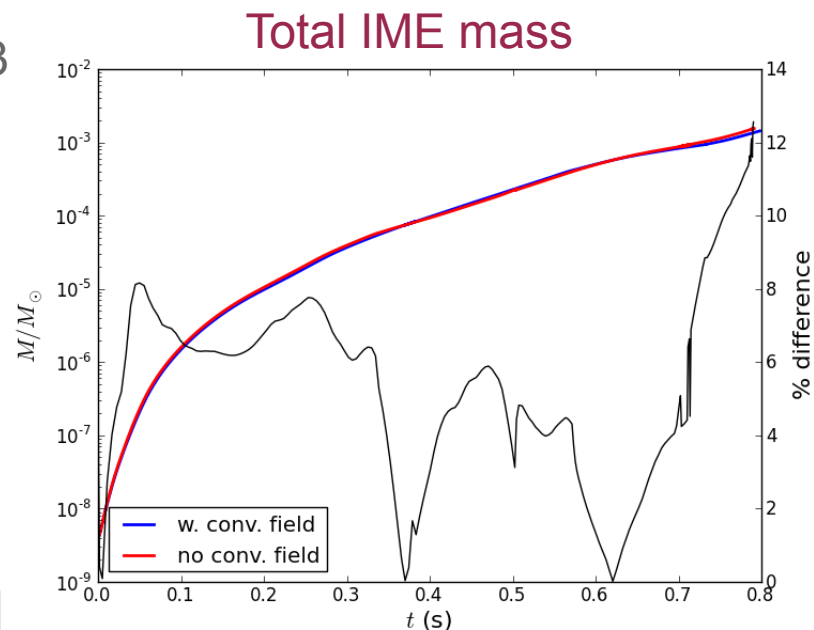
user: cmalone  
Fri May 25 13:07:21 2012

Not much outside...

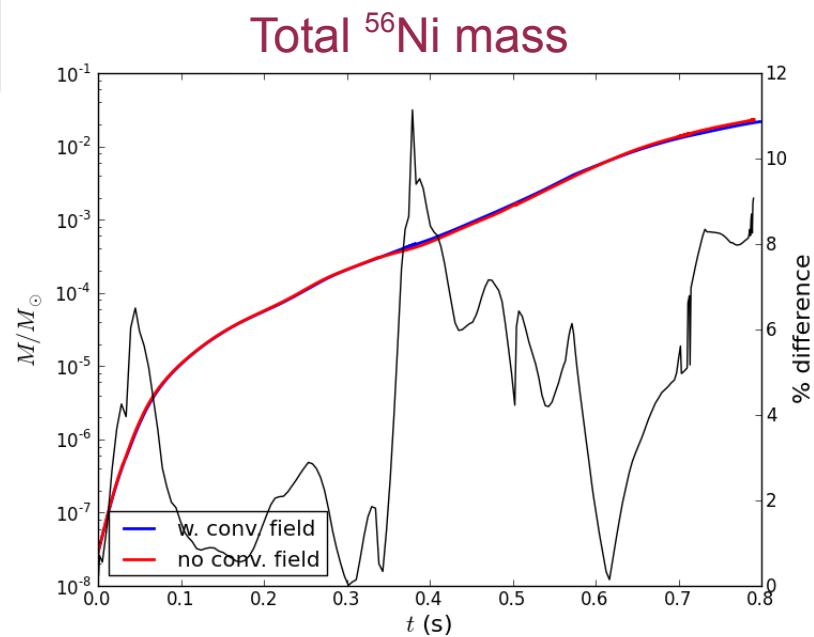
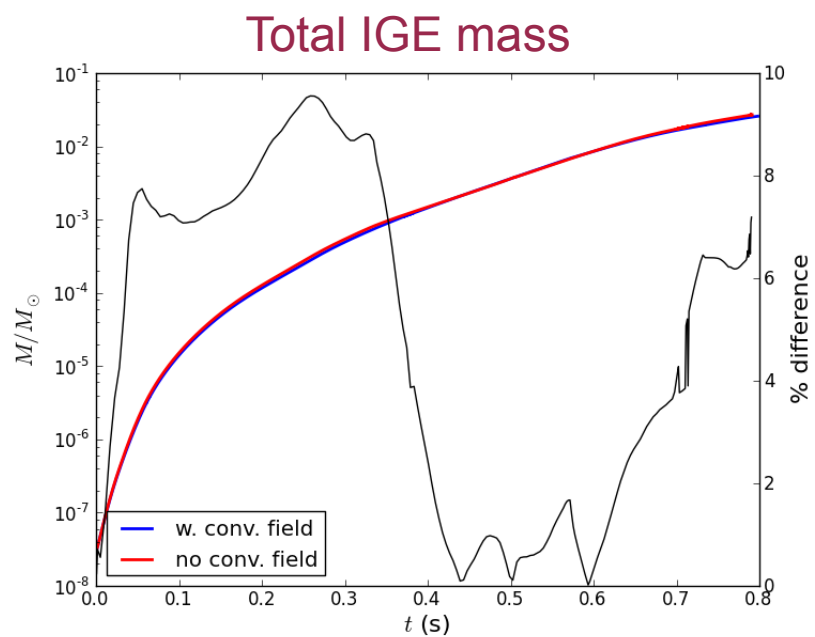
# Effect of Convective Field



Malone+ 2013

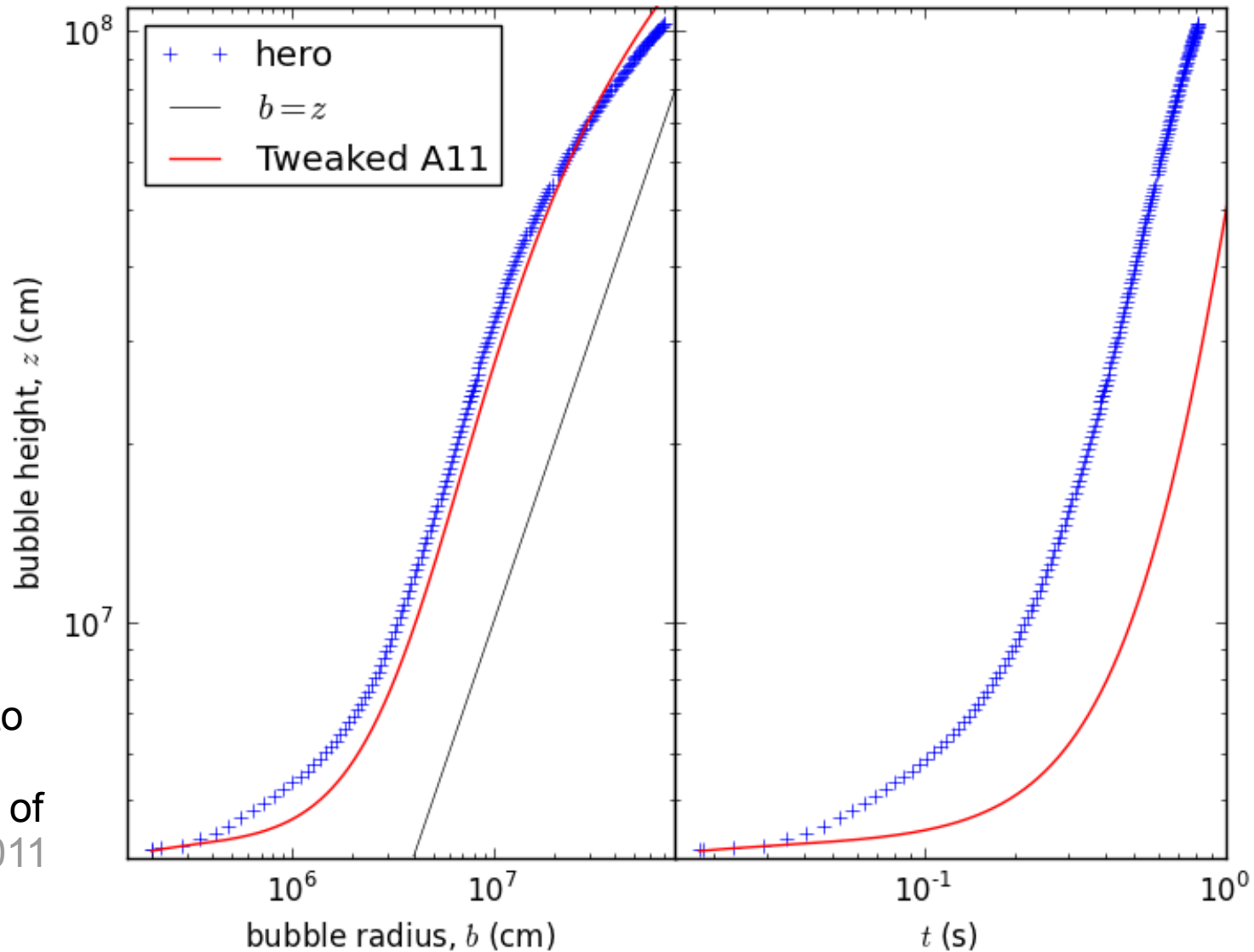


Differences on the 10% level!



# Comparison to Analytic Thermals

Malone+ 2013

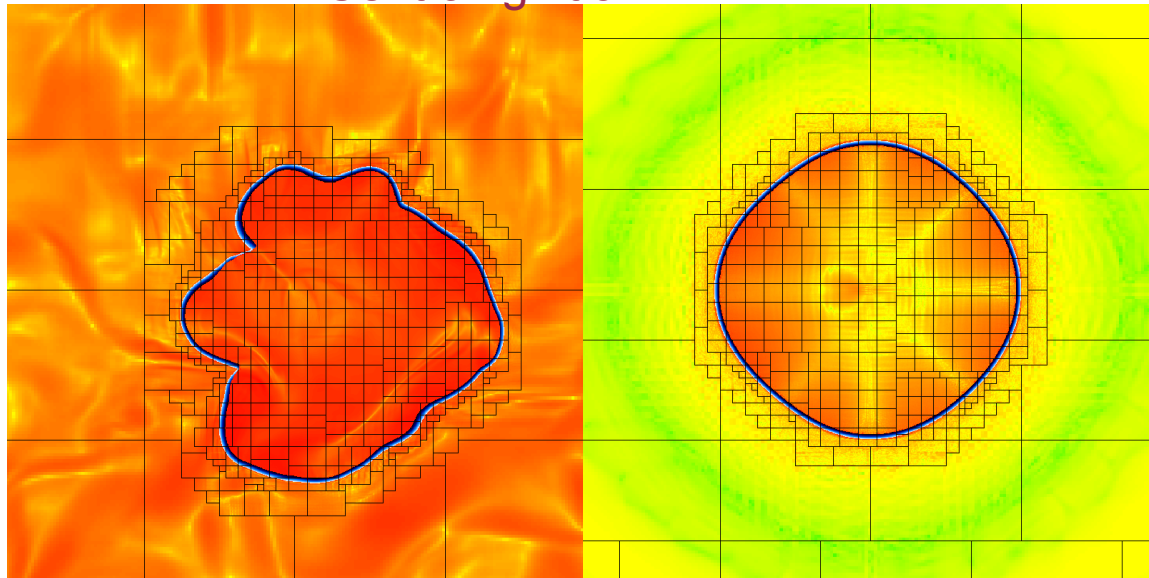


Compared to  
analytic  
prescription of  
Aspden+ 2011

# Ignition Closer To the Center?

Malone+ 2013

Central ignition



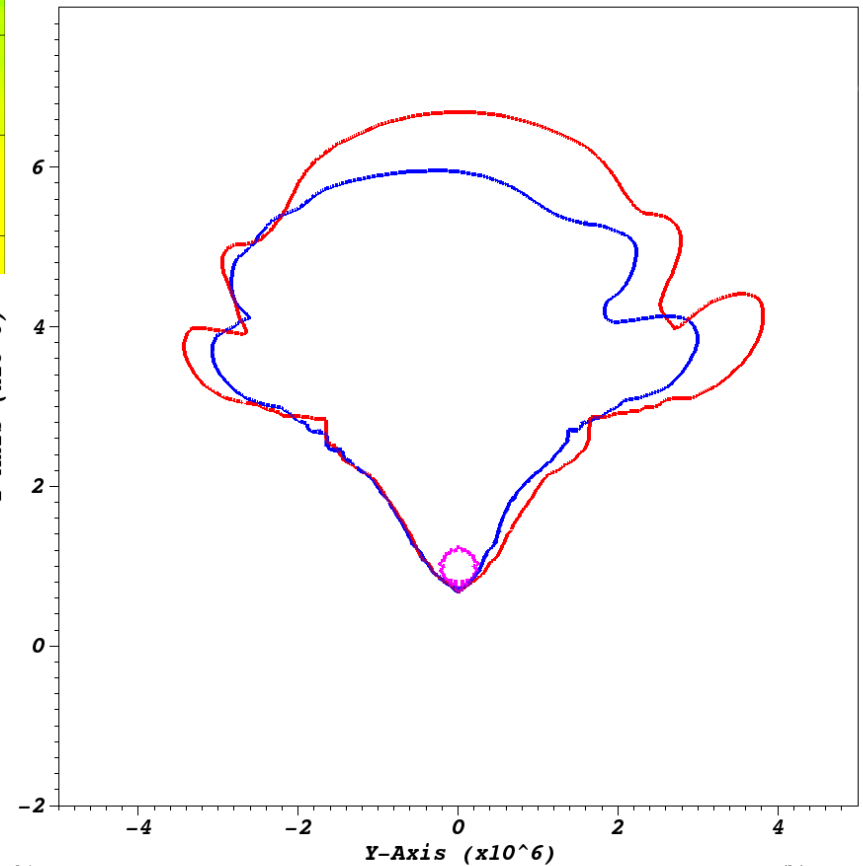
w. convection

no convection

Effect of turbulence on flame evolution stronger near center

Near central ignition tough to burn through to other side

10 km off-center



# Conclusions

- Localized ignition likely off-center (~50 km)
- Ignition occurs in outflow region
- Background turbulence doesn't matter\* unless you ignite near the center
- Most of the turbulence in the vicinity of the flame is within the ash
- A “burn through” seems quite difficult

# Future Work

- More high-resolution simmering/ignition models
- Rotation (requires rework of Maestro algorithm)
- More realistic turbulent flame model (in progress, and see Ma+ 2013)
- Better characterization of turbulence
- Level sets?